

Methods: Mind the Gap  
Webinar Series

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# Designing Stepped Wedge Trials with Continuous Recruitment

Presented by:

Richard Hooper, Ph.D.

Queen Mary University of London, UK



National Institutes of Health  
*Office of Disease Prevention*

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# Introduction



**Katy Bell**  
@KatyJLBell

Equity and evidence during vaccine rollout: stepped wedge cluster randomised trials could help  
[bmj.com/content/372/bm...](https://www.bmj.com/content/372/bm...)

LETTERS

Check for updates

**COVAX ALLOCATION OF COVID VACCINES**

**Equity and evidence during vaccine rollout: stepped wedge cluster randomised trials could help**

Katy J L Bell,<sup>1</sup> Paul Glasziou,<sup>2</sup> Fiona Stanaway,<sup>1</sup> Patrick Bossuyt,<sup>3</sup> Les Inwig<sup>1</sup>

**Herzog and colleagues raise the thorny issue of allocating scarce vaccines, comparing the proportional allocation model with a fair priority model.<sup>1</sup> Regardless of what is used for prioritisation between and within countries, there will be a long period of rollout before most of the world's population are offered vaccination. For groups of equivalent priority, a fair and equitable way to decide on the order of rollout is to use a lottery, or system of random choice.<sup>2</sup> Such randomised sequential rollout of vaccines could be delivered through stepped wedge cluster randomised trials (SW-CRTs).<sup>3</sup> Although constrained by the absence of placebos,<sup>4-6</sup> SW-CRTs might provide valuable information related to uncertainties about different vaccine effects, including:**

- Effectiveness in preventing transmission of SARS-CoV-2 infection from vaccinated patients to others, and whether this differs across genetic variants of the virus including new, more infectious, strains
- Effectiveness in preventing SARS-CoV-2 asymptomatic or paucisymptomatic infection: the Oxford-AstraZeneca vaccine was estimated to have

Competing interests: None declared.

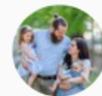
- 1 Herzog LM, Norheim OF, Emanuel EJ, McCoy MS. Covax must go beyond proportional allocation of covid vaccines to ensure fair and equitable access. *BMJ* 2021;372:n4853. doi: 10.1136/bmj.n4853 pmid: 33402340
- 2 Emanuel EJ, Persad G, Upshur R, et al. Fair allocation of scarce medical resources in the time of covid-19. *N Engl J Med* 2020;382:2049-55. doi: 10.1056/NEJMp2005114 pmid: 32202722
- 3 Hemming K, Tallaard M, McKenzie JE, et al. Reporting of stepped wedge cluster randomised trials: extension of the CONSORT 2010 statement with explanation and elaboration. *BMJ* 2018;363:k1614. doi: 10.1136/bmj.k1614 pmid: 30413417
- 4 Rid A, Lipsitch M, Miller FG. The ethics of continuing placebo in SARS-CoV-2 vaccine trials. *JAMA* 2021;325:219-20. doi: 10.1001/jama.2020.25053 pmid: 33315080
- 5 Krause PR, Fleming TR, Longini IM, et al. WHO Ad Hoc Expert Group on the Next Steps for Covid-19 Vaccine Evaluation. Placebo-controlled trials of covid-19 vaccines — why we still need them. *N Engl J Med* 2021;384:e2. doi: 10.1056/NEJMp2033538 pmid: 33264543
- 6 Krause P, Fleming TR, Longini I, Henao-Restrepo AM, Peto R. World Health Organization Solidarity Vaccines Trial Expert Group. Covid-19 vaccine trials should seek worthwhile efficacy. *Lancet* 2020;396:741-3. doi: 10.1016/S0140-6736(20)31821-3 pmid: 32861315
- 7 Voysey M, Clemens SAC, Madhi SA, et al. Oxford COVID Vaccine Trial Group. Safety and efficacy of the ChAdOx1 nCoV-19 vaccine (AZD1222) against SARS-CoV-2: an interim analysis of four randomised controlled trials in Brazil, South Africa, and the UK. *Lancet* 2021;397:99-111. doi: 10.1016/S0140-6736(20)32661-1 pmid: 33306989
- 8 Polack FP, Thomas SJ, Kitchin N, et al. A591001 Clinical Trial Group. Safety and efficacy of the BNT162b2 mRNA covid-19 vaccine. *N Engl J Med*

BMJ: first published as 10.1136/bmj.n435 on 12 February 2021. Downloaded from http://w



**Dr. Bertha Hidalgo** @berthahidalgo · Jan 19  
I just want to know why we have zero randomized trials on dresses with pockets.

135 275 3,496



**Dr. Catherine Bulka** @DrCatherineB · Jan 19  
Double-blinding would be a real problem because whenever complimented on a dress with pockets, the automatic response is always “thanks, it has POCKETS!”

2 112



**Eric Lofgren**  
@GermsAndNumbers

Replying to @DrCatherineB and @berthahidalgo

Stepped wedge design. Eventually, all dress wearers get pockets.

We have the methods to address this balancing ethics and statistical efficiency.

2:27 AM · Jan 19, 2022 · Twitter Web App

# What is a stepped wedge trial?

- Usually cluster randomised
- Clusters are randomised, not to one treatment condition or another, but to a **sequence** of treatment conditions over an extended interval of time
- In a sequence, cross-over is **unidirectional**: you cannot cross from the intervention condition back to the control condition

# What are the advantages of a stepped wedge trial?

Reputed advantage:

- Everyone gets the intervention

# What are the advantages of a stepped wedge trial?

Real advantages are two-fold:

- Statistical efficiency (in some cases)
- Practicality: there may not be “enough” of the intervention to deliver to half the clusters simultaneously

# The Gambia Hepatitis Intervention Study<sup>1</sup>

The Gambia Hepatitis Study Group<sup>2</sup>

## ABSTRACT

The Gambia Hepatitis Intervention Study is a large-scale vaccination project in The Gambia, initiated in July 1986, in which the introduction of national hepatitis B (HBV) vaccination of young infants progressively over a 4-year period is proposed. During this time it is anticipated that about 60,000 infants will receive a course of HBV vaccine and a similar number will not receive the vaccine. All children in the study will receive the normal childhood vaccinations. Identification data for each child will be collected and stored with information on their vaccination records. A national surveillance system will be set up to detect new cases of hepatocellular cancer and other chronic liver diseases over a period of 30 to 40 years. An attempt will be made to trace each case, of relevant age, to determine if they are included in the HBV vaccination study. In this way, the efficacy of HBV vaccine in the prevention of HCC and chronic liver diseases will be evaluated. Details of the study design are discussed.

## INTRODUCTION

Chronic liver diseases and HCC<sup>3</sup> are major health problems

infection the HBsAg persistent carrier state is a major risk factor for HCC as well as for a high proportion of cases of chronic liver diseases.

The development of safe and effective subunit vaccines against HBV offers the potential for preventing a high incident cancer and for reducing the significant morbidity and mortality attendant on the other chronic sequelae of HBV infection.

In this paper we outline the design of a long-term study which has started recently in The Gambia to evaluate the impact of HBV vaccination on the incidence of HCC and other liver diseases.

## NEED FOR A CONTROLLED VACCINE TRIAL

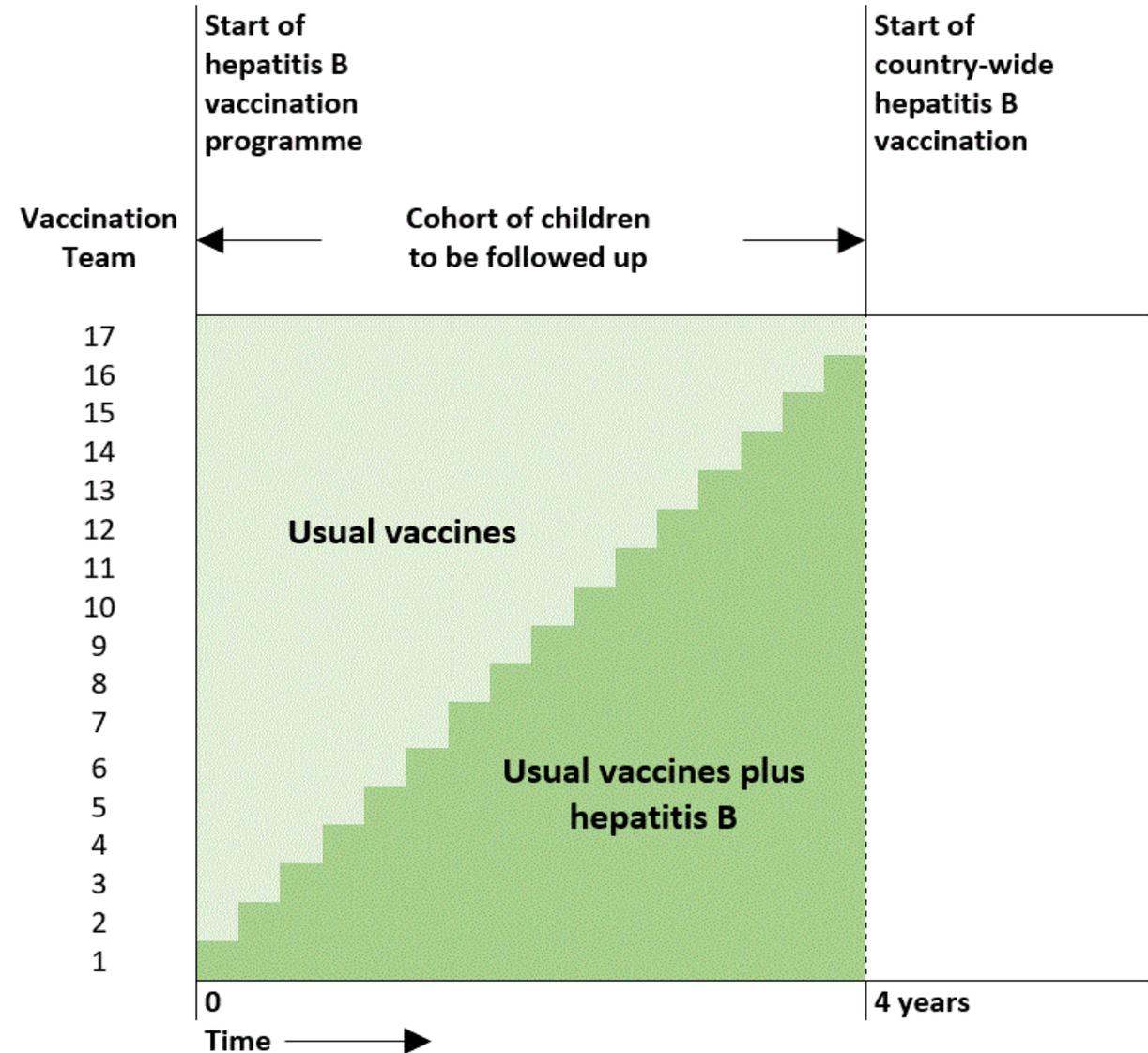
A number of trials have been conducted to assess the protective effect of the currently available plasma-derived HBV vaccines against HBV infections. These trials, in selected high-risk groups (*e.g.*, homosexuals, hospital personnel), have shown that

[CANCER RESEARCH 47, 5782–5787, November 1, 1987]

# The Gambia Hepatitis Intervention Study

The Gambia Hepatitis Study Group<sup>2</sup>

17 regional vaccination teams  
randomised to different schedules  
for rolling out hep B vaccine for  
newborn infants, in a stepped wedge



# A typology for stepped wedge trial designs

# A typology for stepped wedge trial designs

First we came  
up with a typology.



People who use  
the term typology

People who don't  
use the term typology

fresh spectrum  
stepped wedge hog. blog

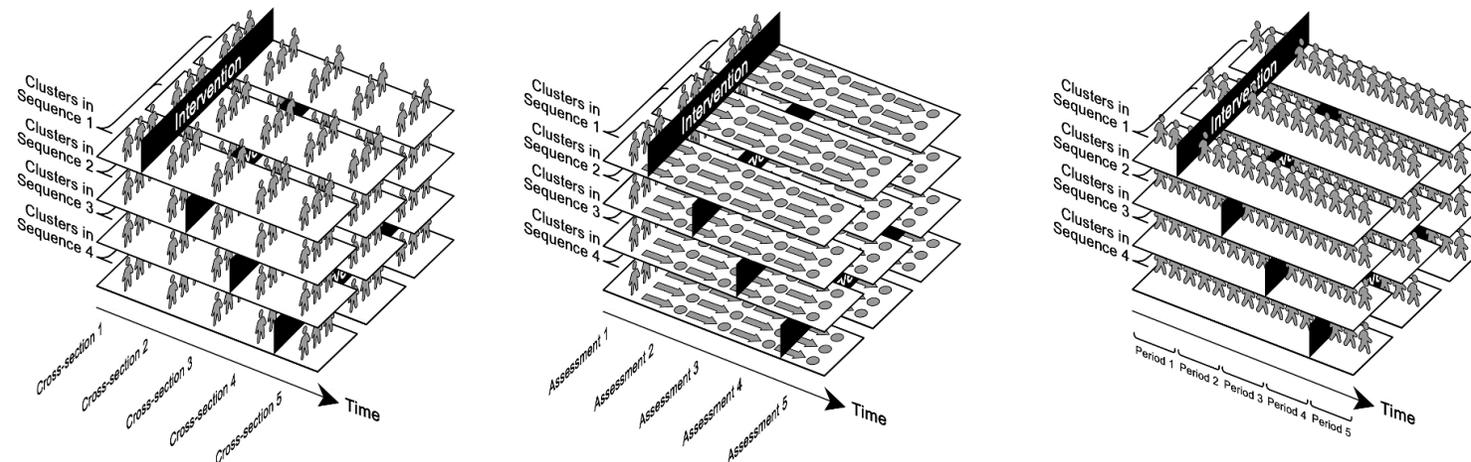
ORIGINAL ARTICLE

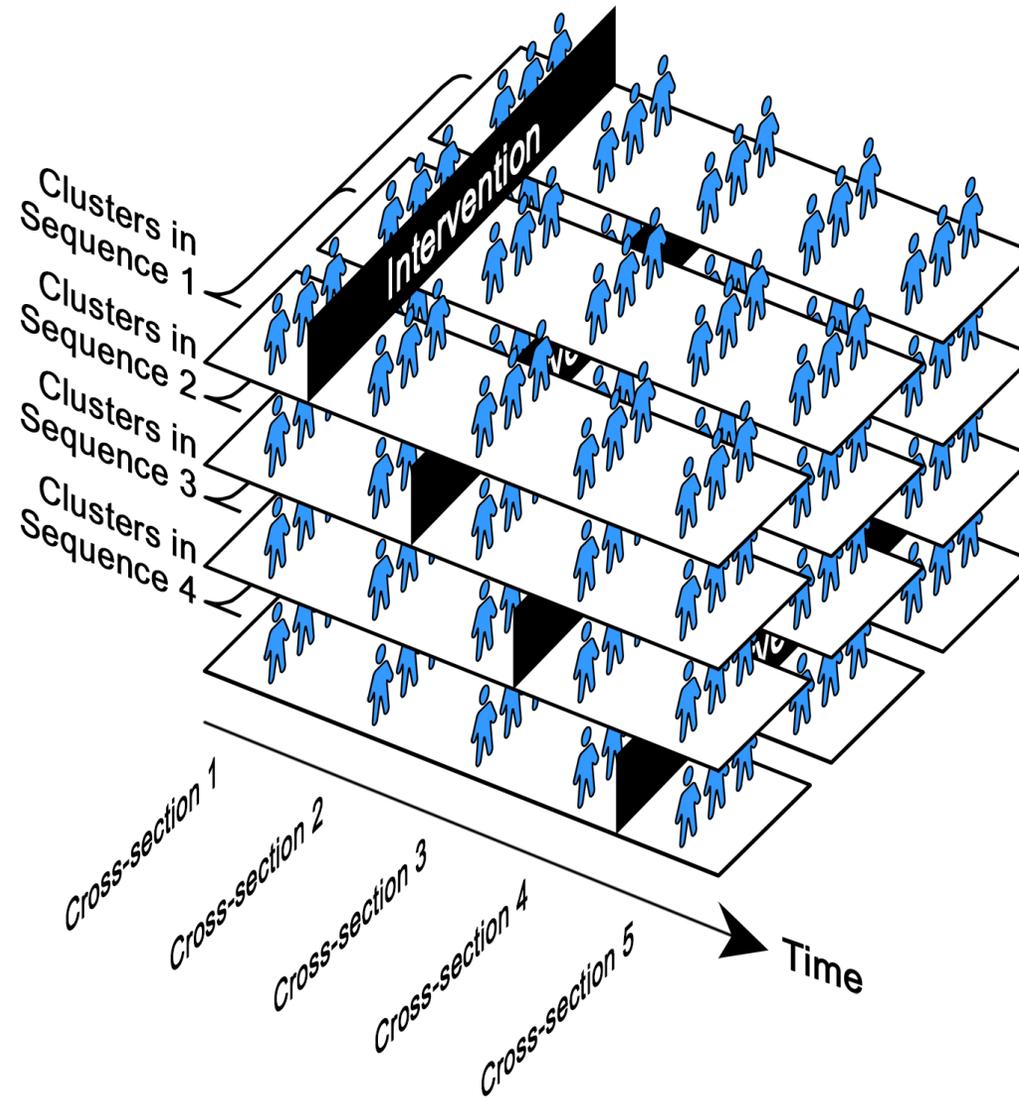
# Key concepts in clinical epidemiology: Stepped wedge trials

Richard Hooper\*

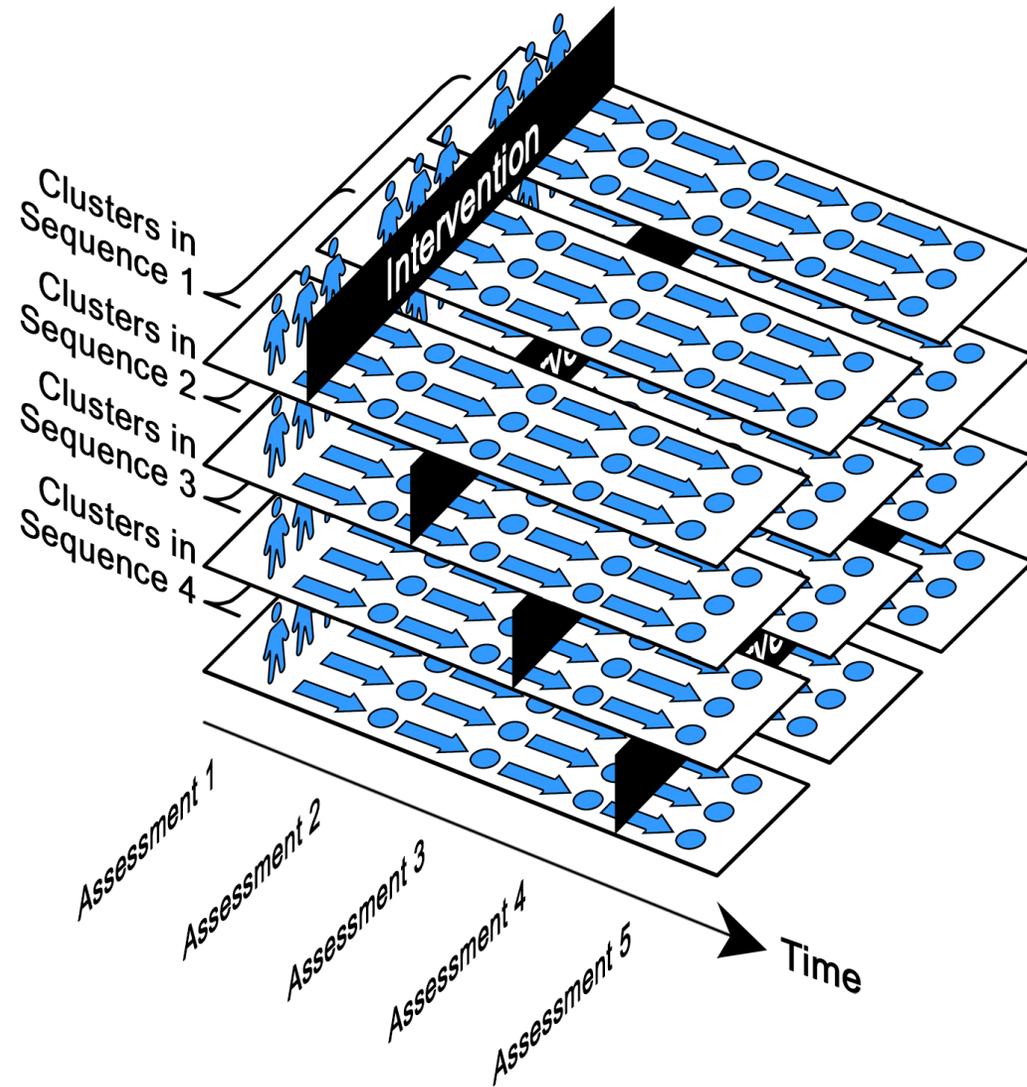
*Institute of Population Health Sciences, Queen Mary University of London, London, UK*

Received 16 March 2021; Received in revised form 10 April 2021; Accepted 13 April 2021; Available online 20 April 2021



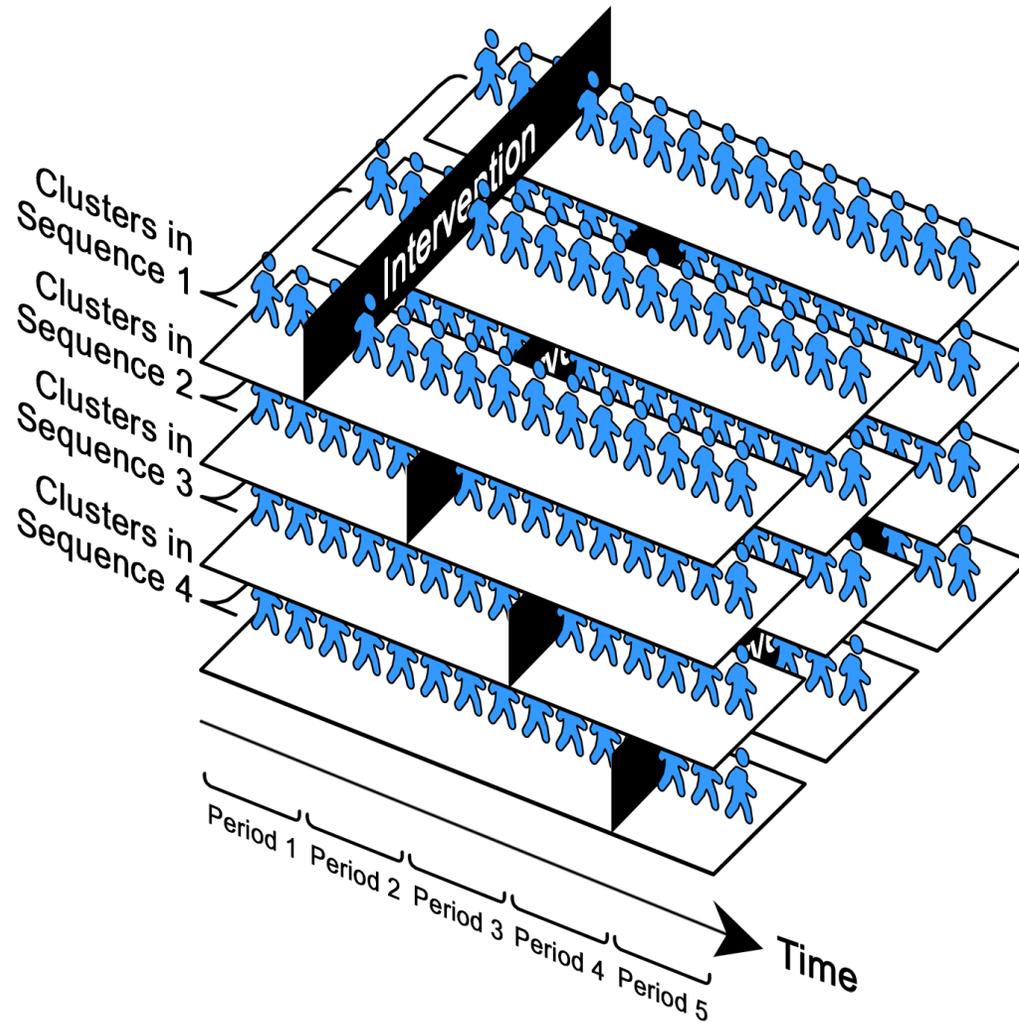


# Repeated cross-section

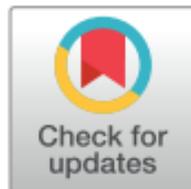


Closed  
cohort

# Continuous recruitment



New ways of thinking



**COMMENTARY**

**Stepped wedge trials with continuous recruitment require  
new ways of thinking**

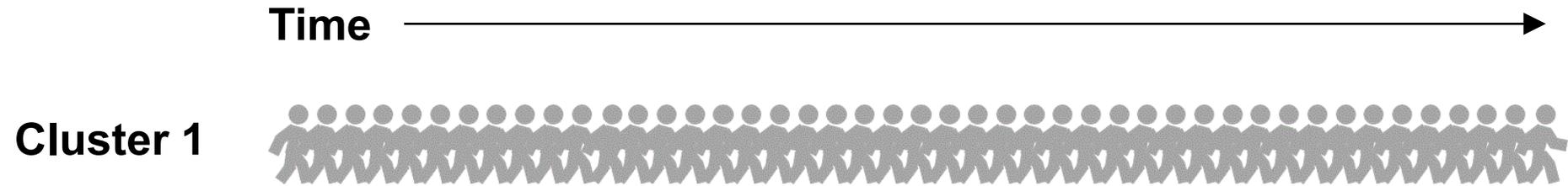
**Richard Hooper<sup>a,\*</sup>, Andrew Copas<sup>b</sup>**

<sup>a</sup>*Centre for Primary Care & Public Health, Queen Mary University of London, London, UK*

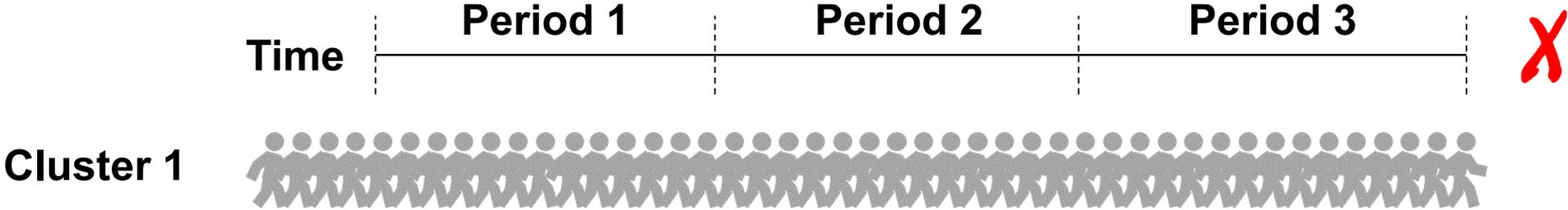
<sup>b</sup>*MRC Clinical Trials Unit, University College London, London, UK*

Accepted 29 May 2019; Published online 11 June 2019

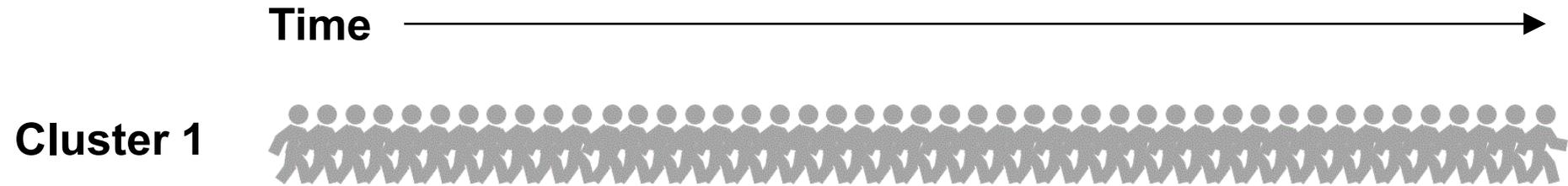
# Continuous recruitment in a cluster



# Continuous recruitment in a cluster



# Continuous recruitment in a cluster



# New ways of thinking



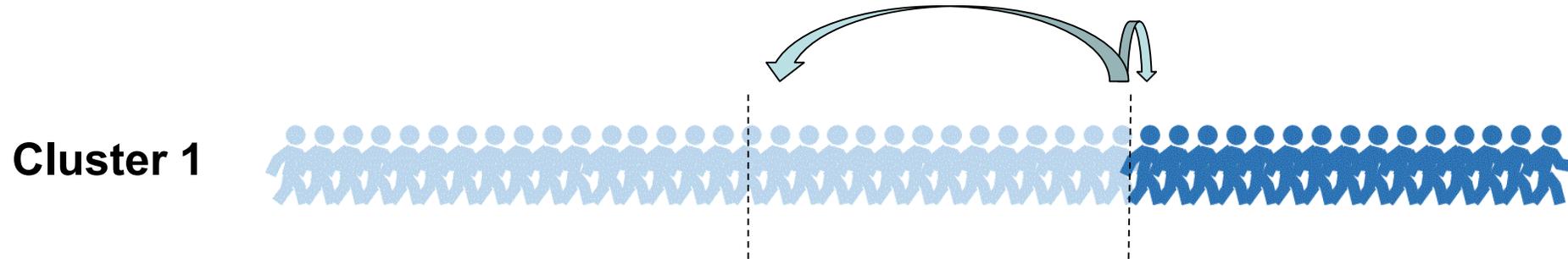
# 1. Crossing over to the intervention

Cluster 1



- Recruitment under control condition
- Recruitment under intervention condition

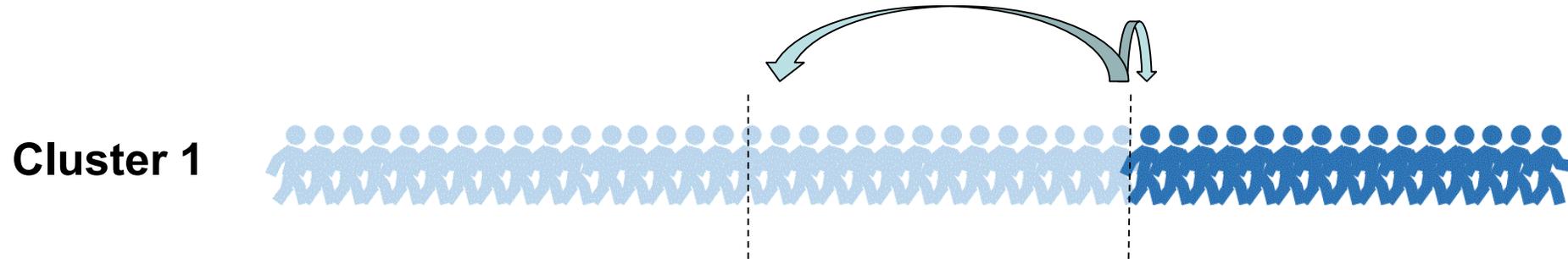
## 2. Modelling the cluster correlation



Longitudinal cluster randomised trials sometimes assume the intracluster correlation is exchangeable within “periods” of time.

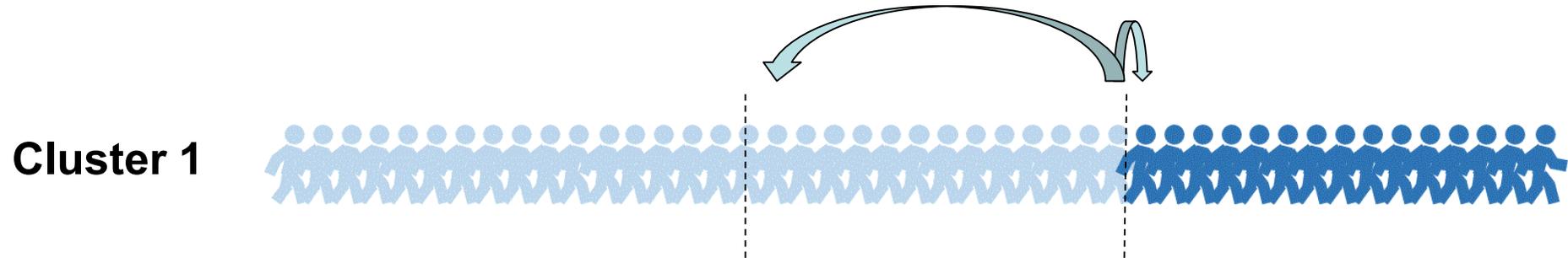
But when recruitment is continuous, which outcomes will be more closely correlated?

## 2. Modelling the cluster correlation



Makes more sense to assume the ICC decays with increasing separation in time

## 2. Modelling the cluster correlation

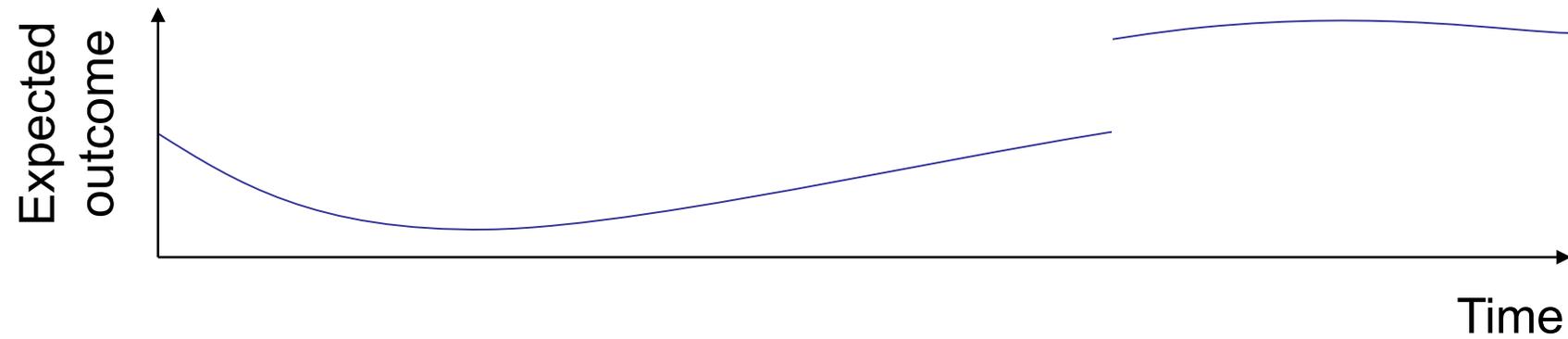


Makes more sense to assume the ICC decays with increasing separation in time

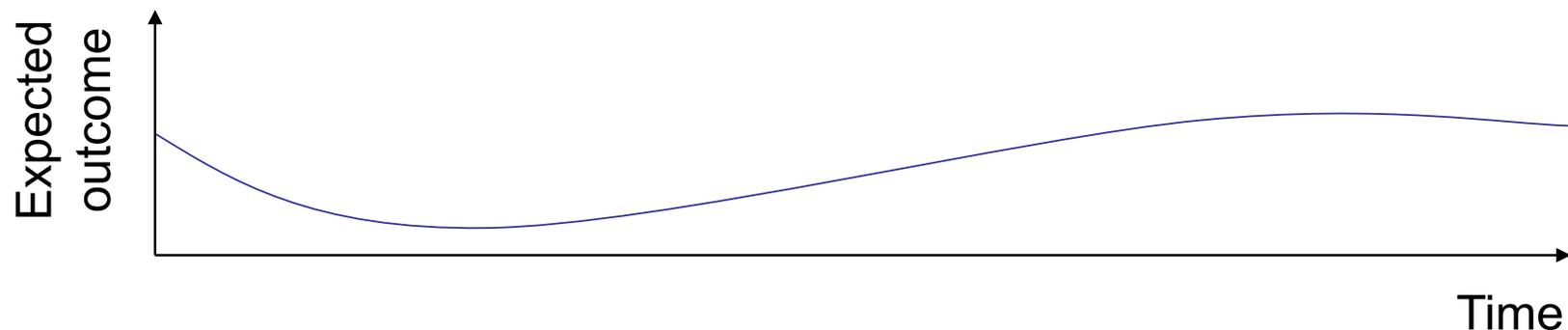
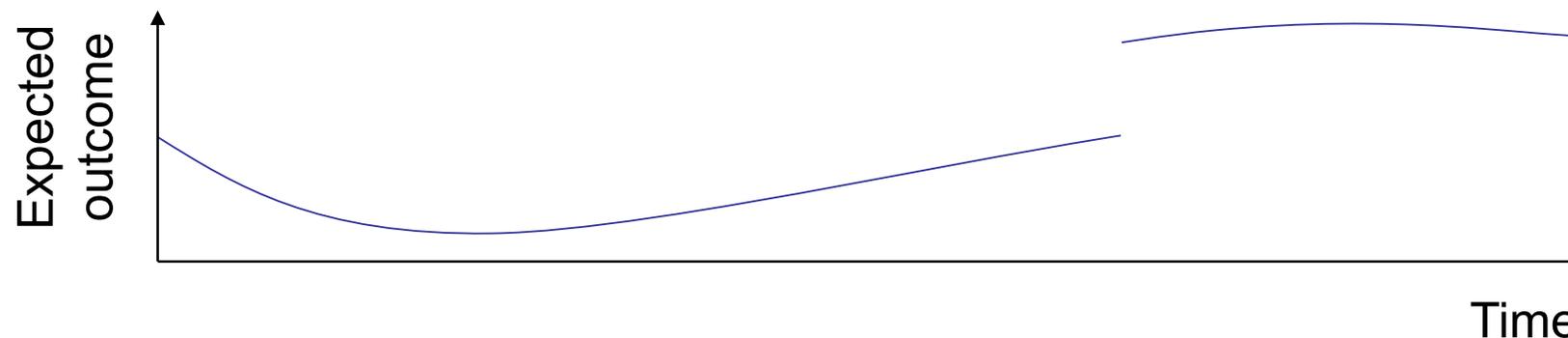
$ICC = \rho\tau^{|t_2-t_1|}$ ,  $t = 0$  at the start of the trial, and  $t = 1$  at the end

### 3. Modelling the underlying effect of time

Cluster 1



### 3. Modelling the underlying effect of time



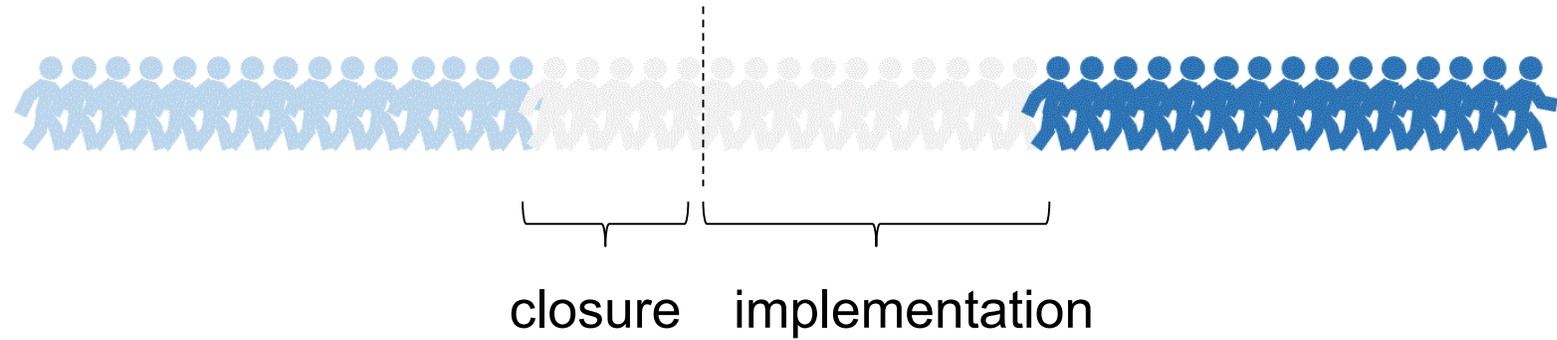
# 4. Allowing for a transition period

Cluster 1

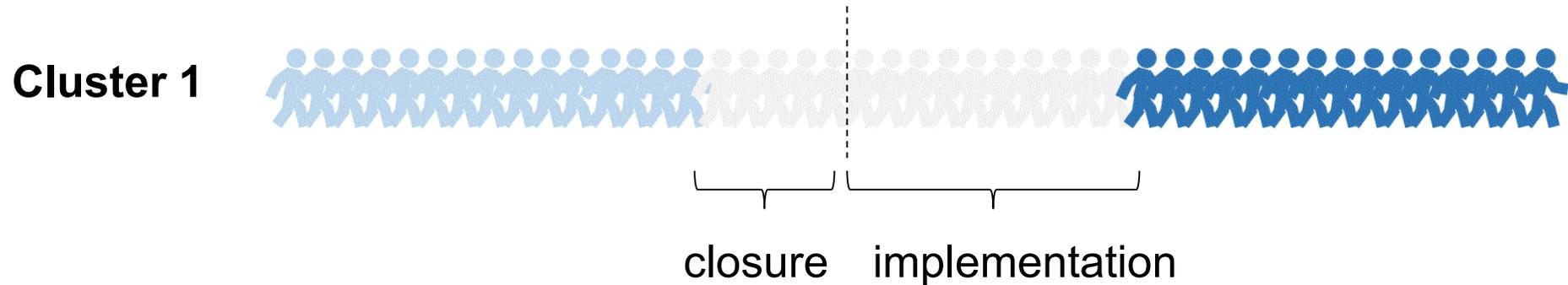


## 4. Allowing for a transition period

Cluster 1



## 4. Allowing for a transition period



The closure period should be long enough for the last participant recruited under the control condition to have left the cluster or to have been assessed

# 5. Incomplete designs

Cluster 1



You may not want to recruit every available participant  
(e.g. if there is a financial or ethical cost per participant)

# 5. Incomplete designs



Some methods

# Statistical model

Participant  $i$  in cluster  $k$  is recruited at time  $t_{ik}$

Cluster  $k$  crosses from control to intervention at time  $t_k^*$

Model for continuous outcome  $Y_{ik}$  is

$$Y_{ik} = T(t_{ik}) + \delta \cdot H(t_{ik} - t_k^*) + e_{ik}$$

where  $T(t)$  is the effect of time common to all clusters,  $H(t)$  is the step function, and  $\delta$  is the intervention effect

# Generalised least squares estimation

Write outcomes  $Y_{ik}$  as column vector  $\mathbf{Y}$

$$\mathbf{Y} = \mathbf{Z}\boldsymbol{\theta} + \mathbf{e}, \quad \mathbf{e} \sim N(\mathbf{0}, \mathbf{V})$$

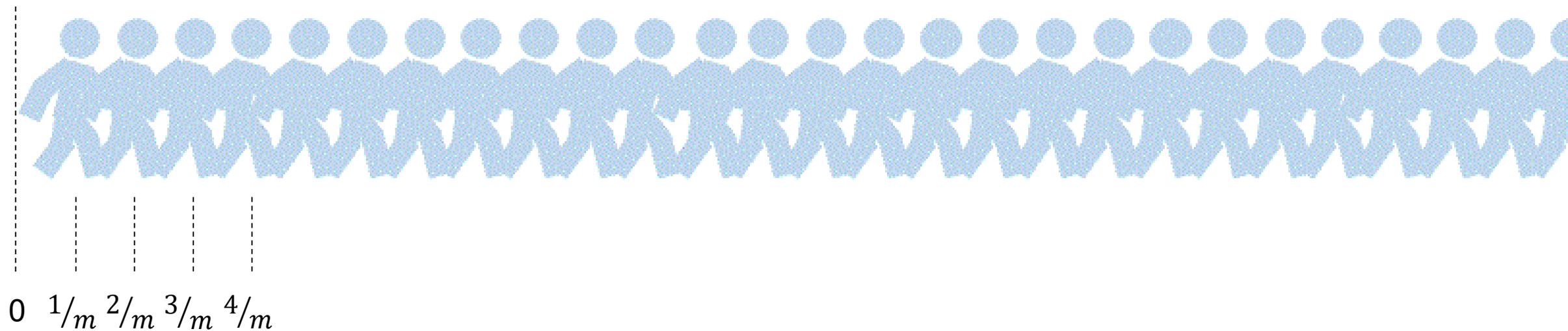
where  $\boldsymbol{\theta}$  is a vector of parameters, including  $\delta$  and the parameterisation of the time effect  $T(t)$

Then the variance of the GLS estimator for  $\boldsymbol{\theta}$  is

$$\text{Var}(\hat{\boldsymbol{\theta}}) = (\mathbf{Z}'\mathbf{V}^{-1}\mathbf{Z})^{-1}$$

# Simplification/regularisation of recruitment times

Participant  $i$  in cluster  $k$  is recruited at time  $t_{ik}$



# Some design problems

- Cluster randomised trials with a prospective baseline

Article

**CLINICAL  
TRIALS**

# Optimal design of cluster randomised trials with continuous recruitment and prospective baseline period

Richard Hooper<sup>1</sup>  and Andrew J Copas<sup>2</sup> 

*Clinical Trials*

2021, Vol. 18(2) 147–157

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 SAGE

?

Cluster 1



Cluster 2



Cluster  $J$



Cluster  $J+1$

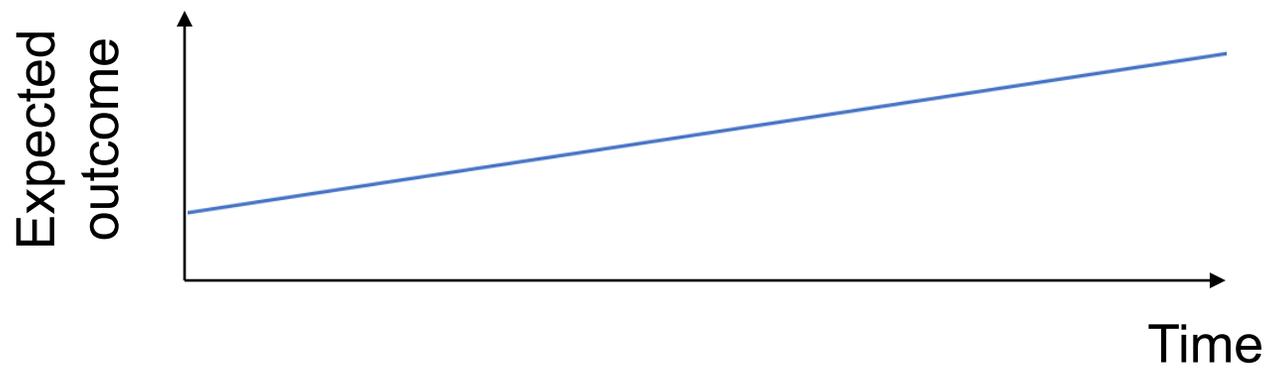
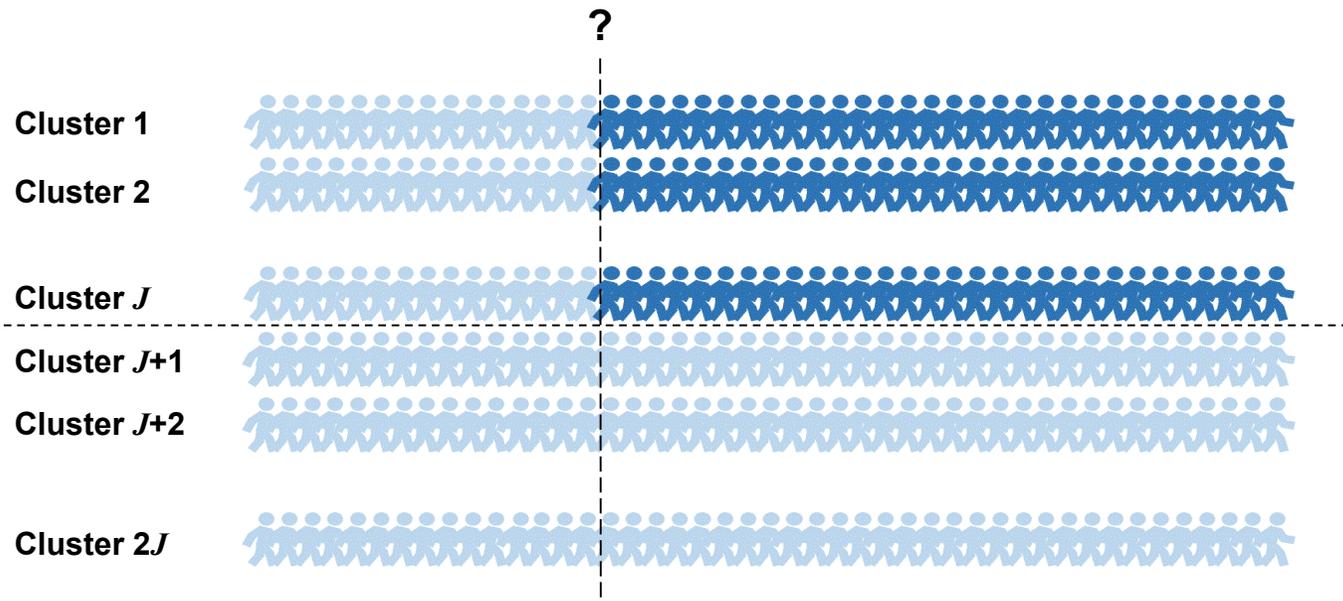


Cluster  $J+2$



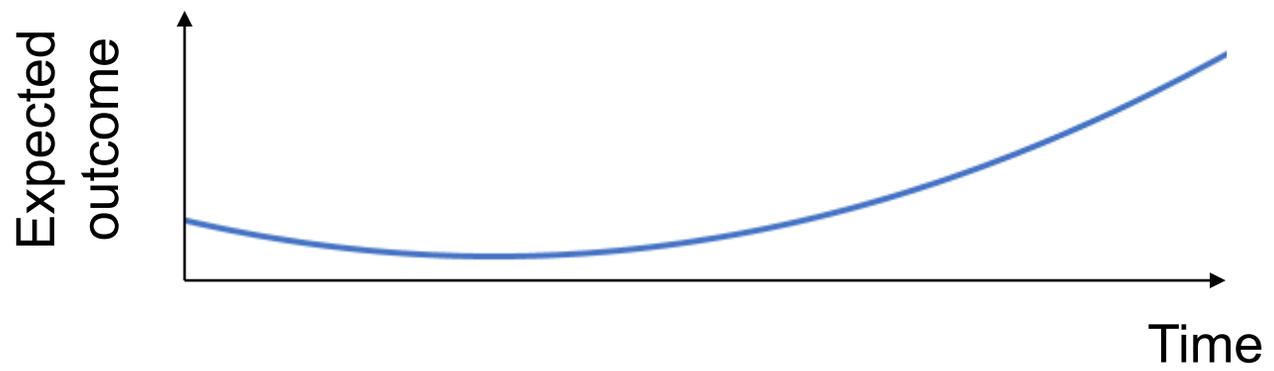
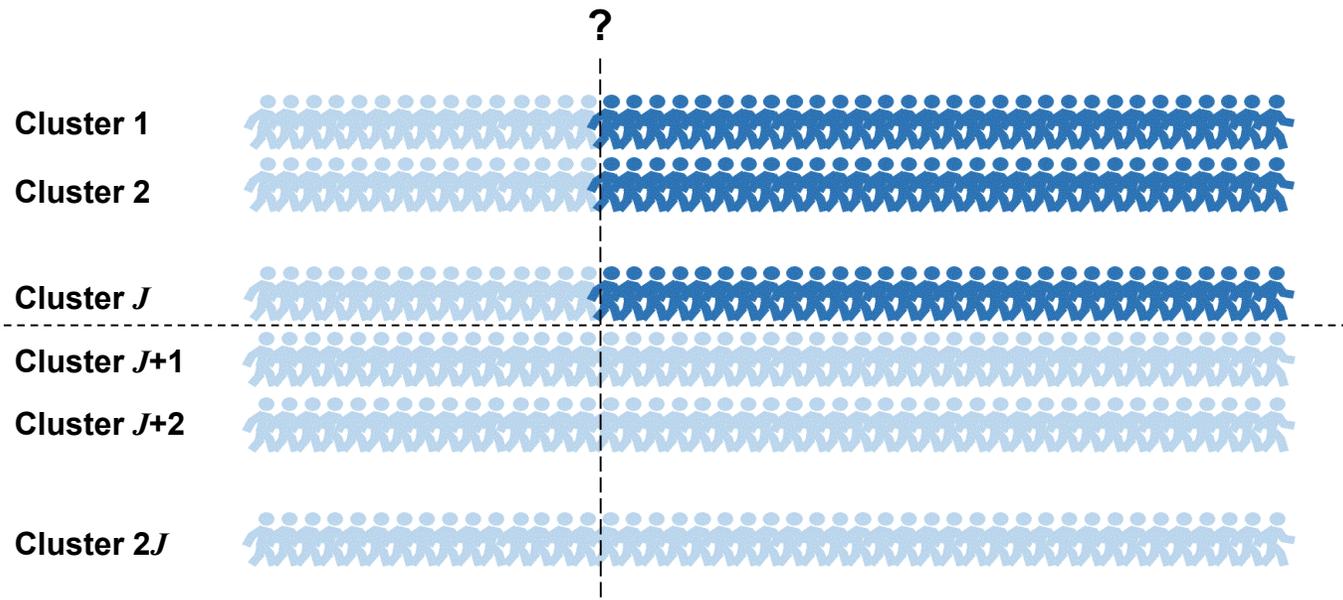
Cluster  $2J$



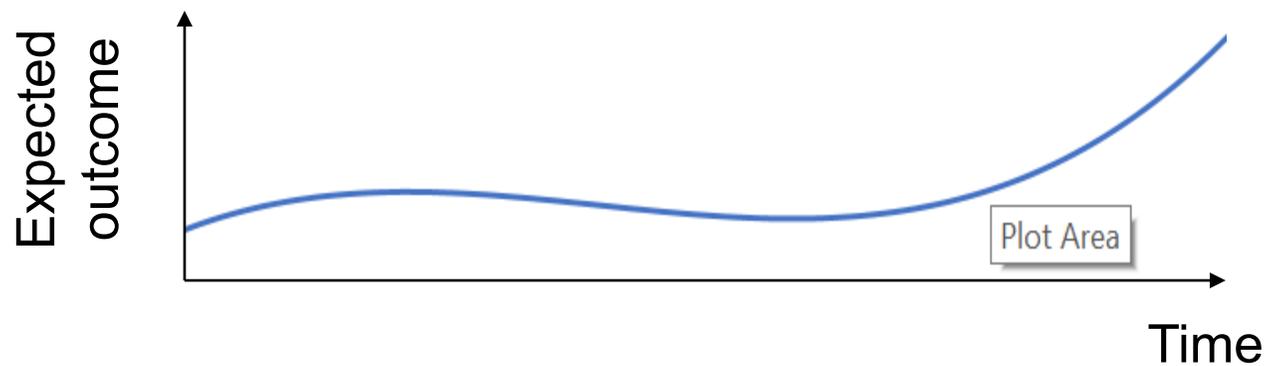
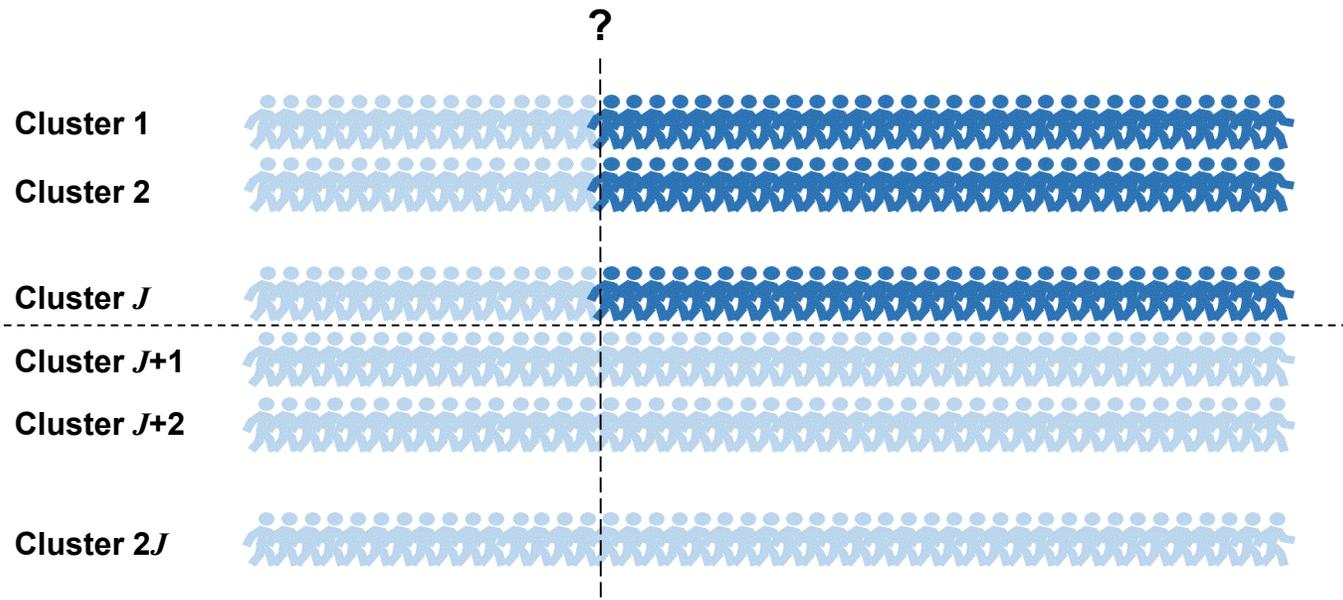


Linear effect of time

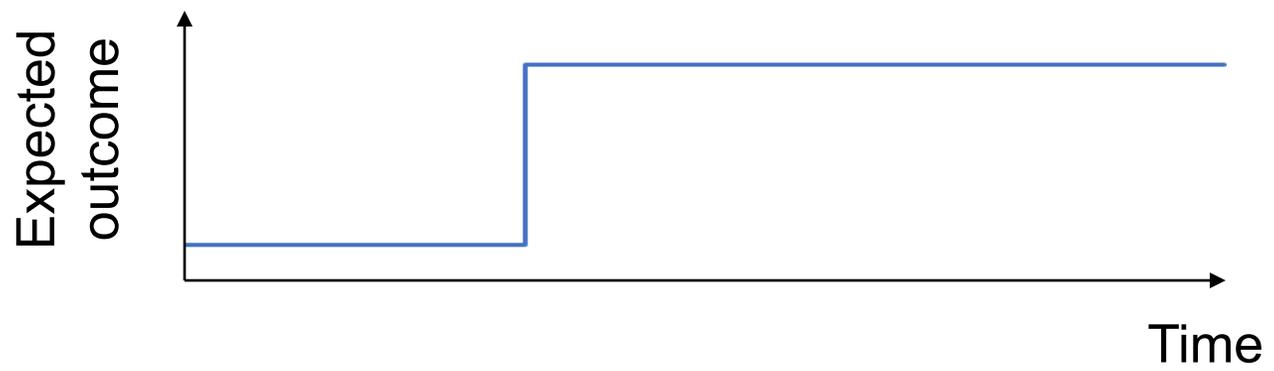
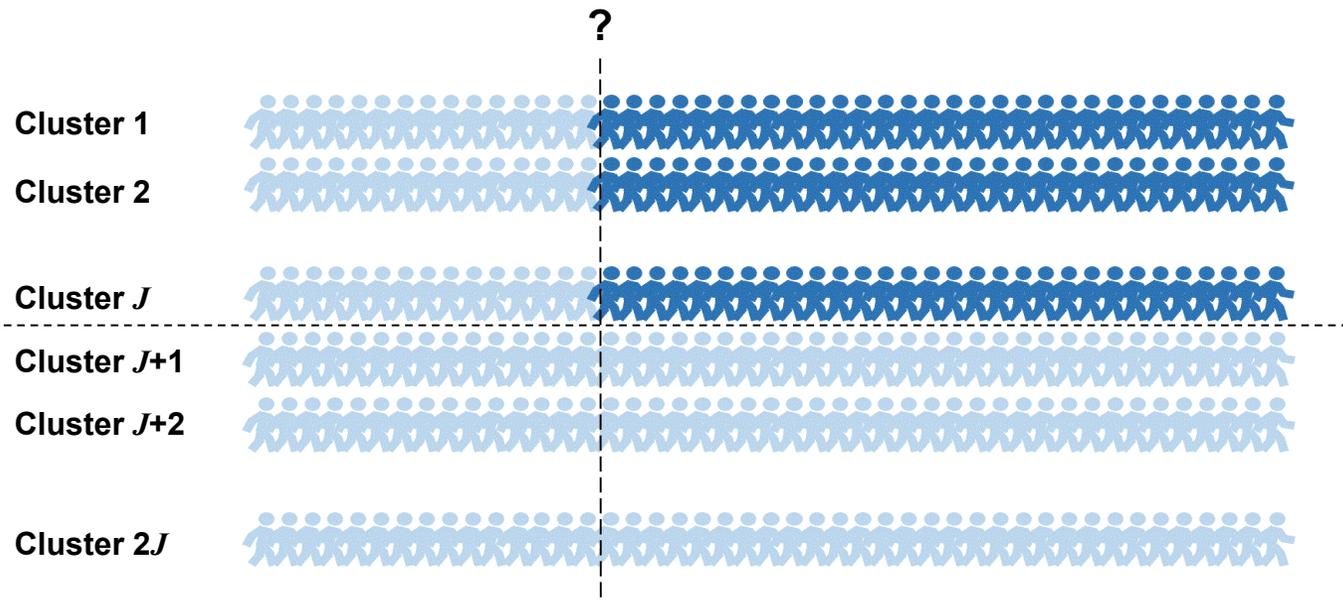




Quadratic effect of time



Cubic effect of time



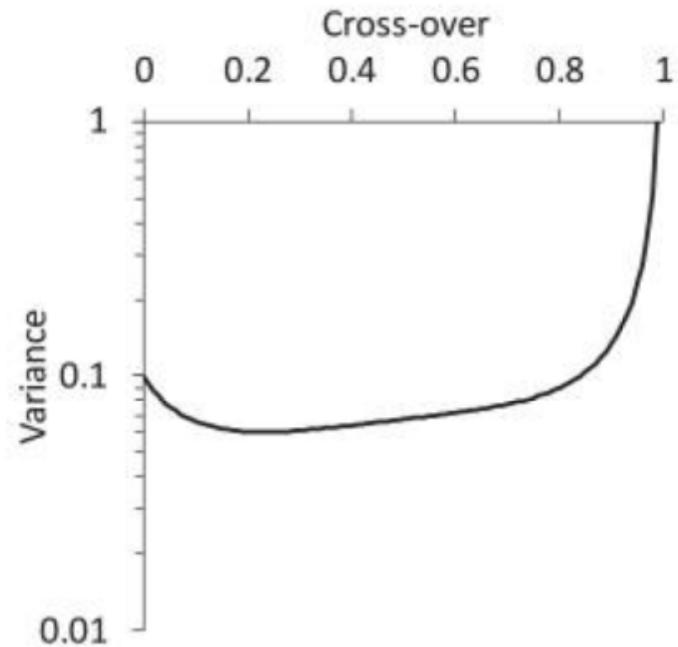
Discontinuous effect of time

# Variance of treatment effect estimator

$$m = 100$$

$$\rho = 0.05$$

$$\tau = 0.5 \quad \text{linear}$$



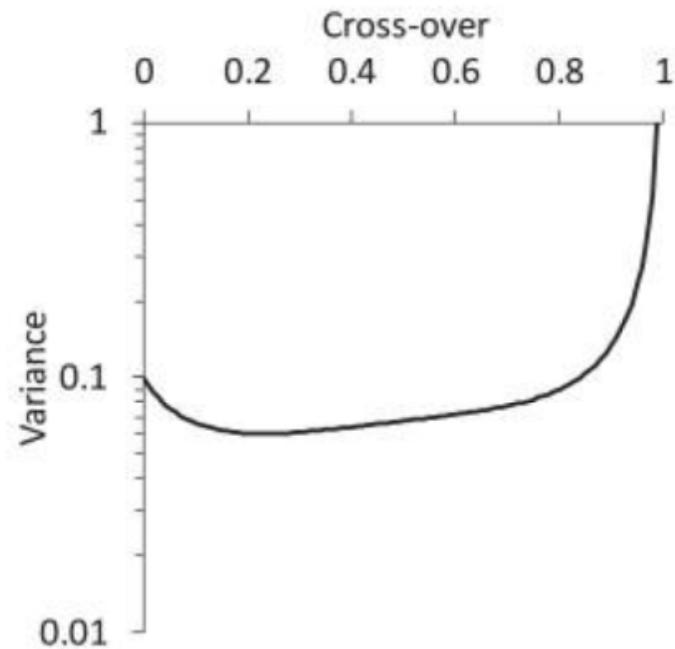
# Variance of treatment effect estimator

$m = 100$

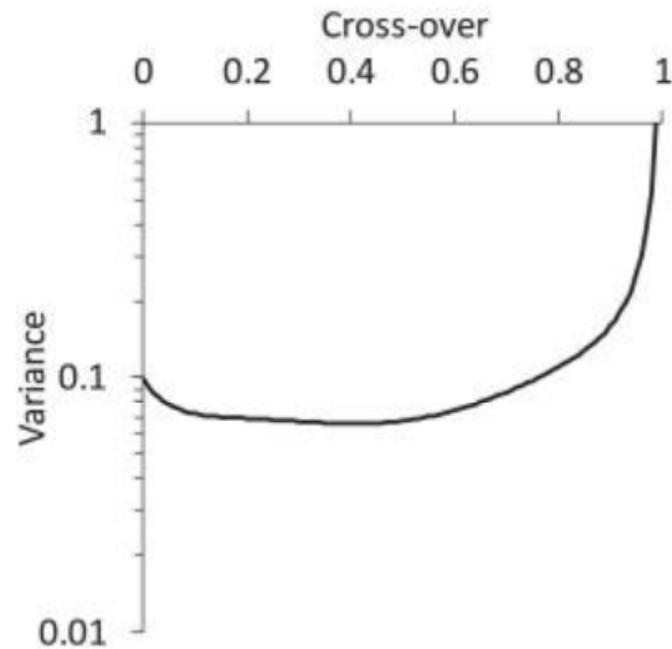
$\rho = 0.05$

$\tau = 0.5$

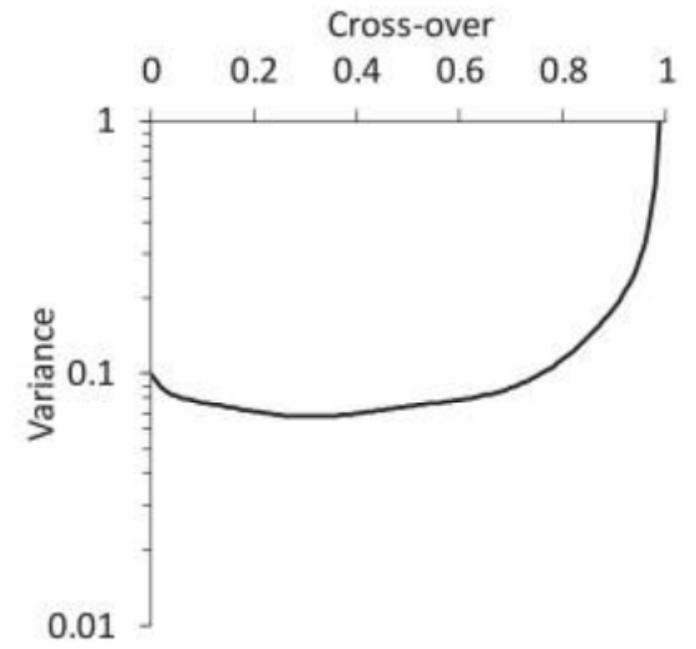
linear



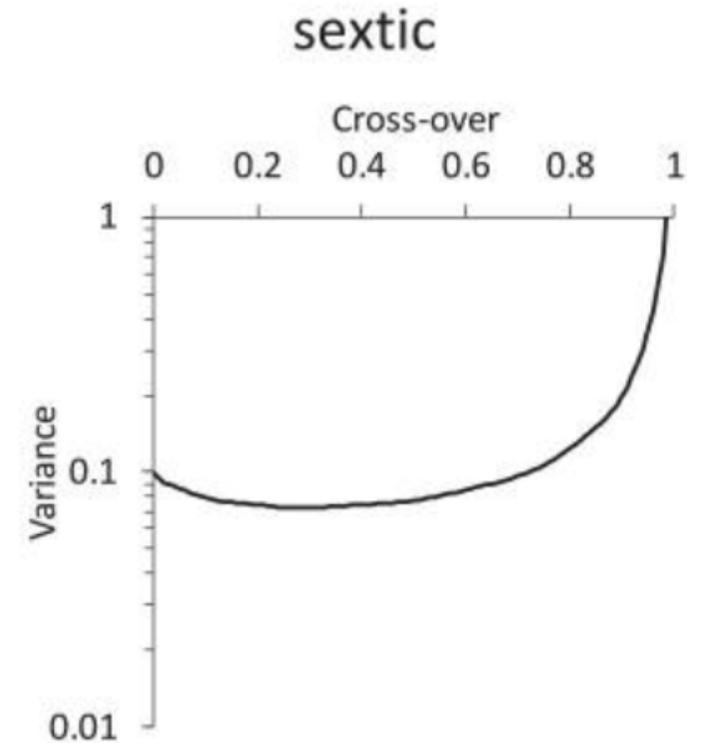
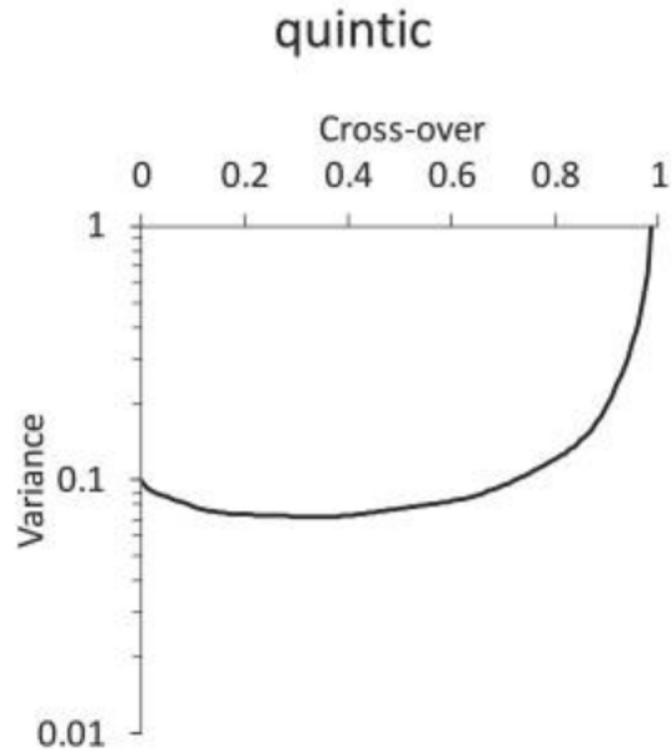
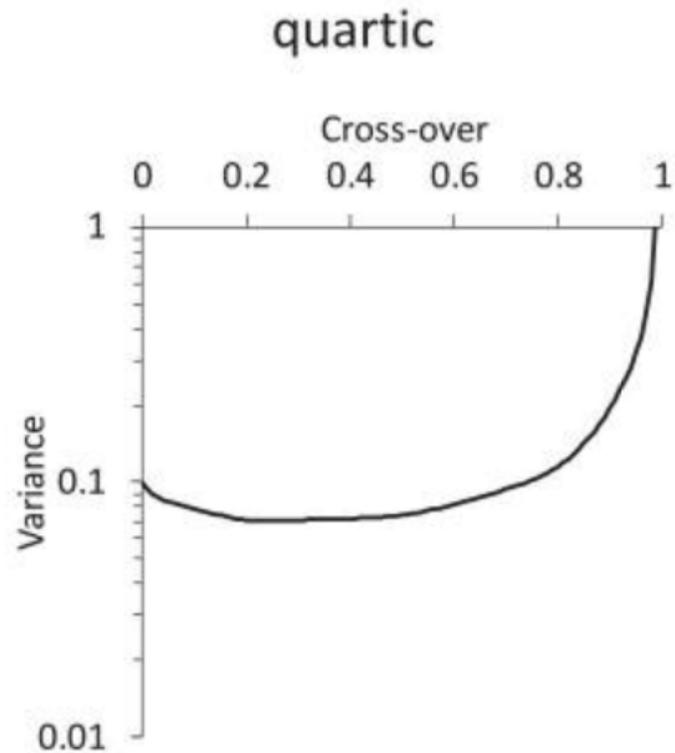
quadratic



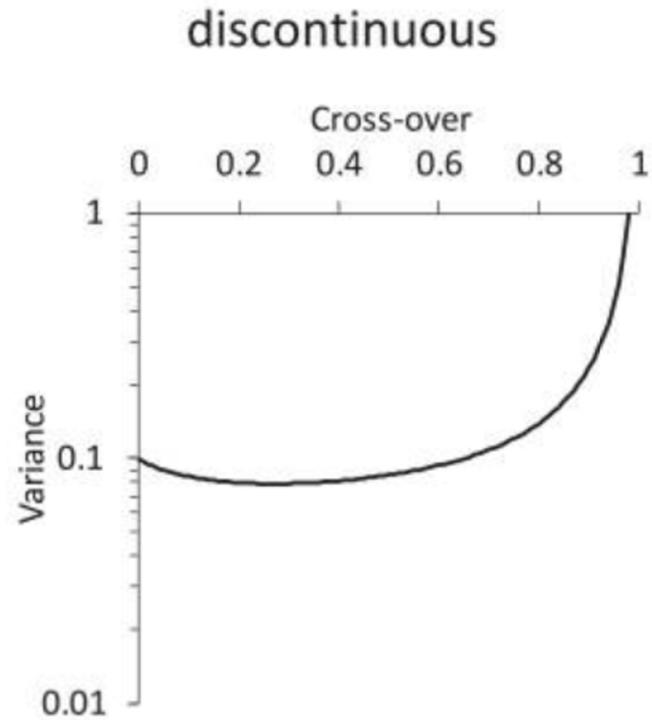
cubic



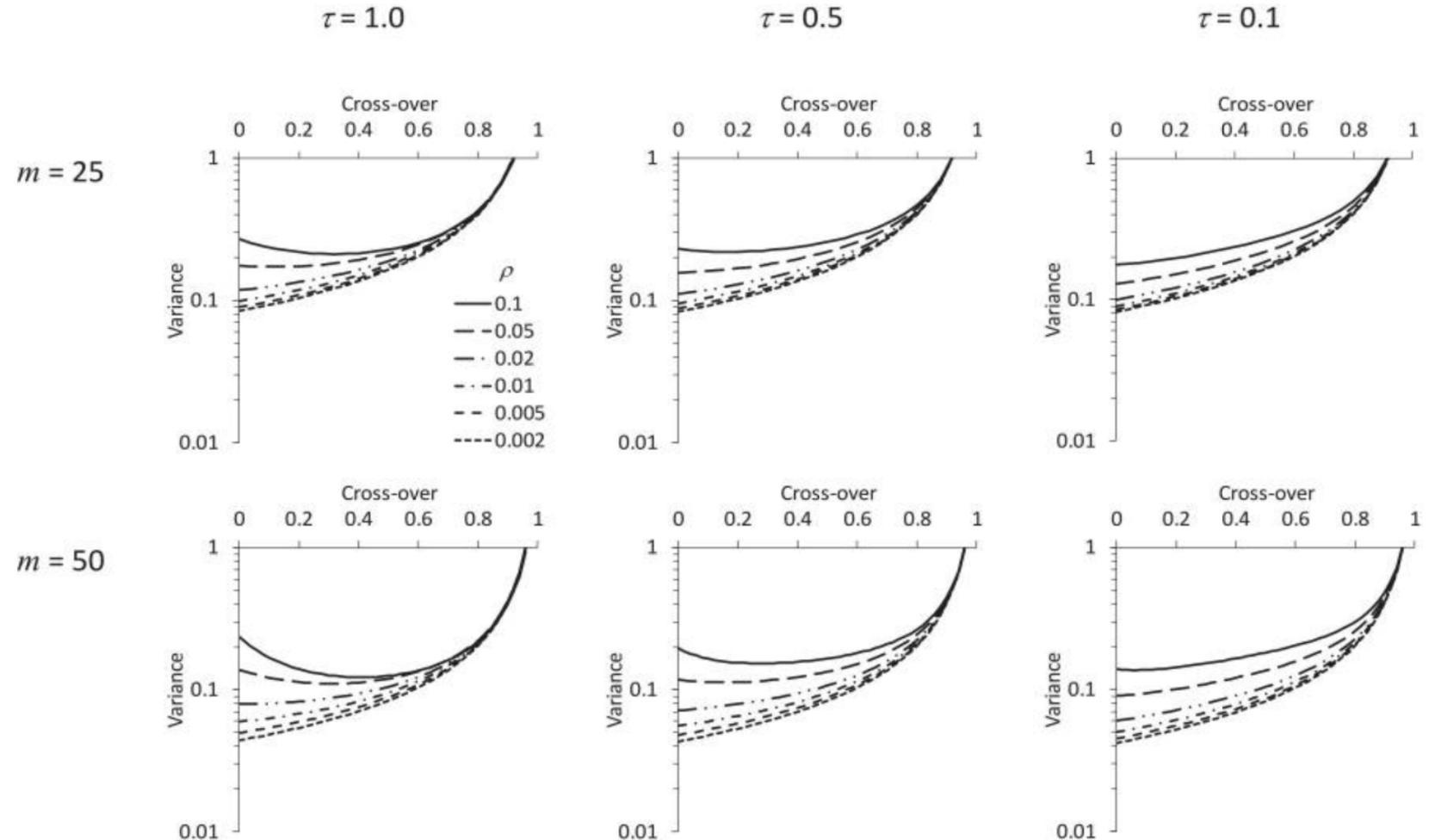
# Variance of treatment effect estimator



# Variance of treatment effect estimator



# Variance of treatment effect estimator



## Simple rule of thumb

You will not go far wrong by choosing between no baseline period, or a baseline period half the length of the recruitment period, whichever leads to the smaller variance

## Simple rule of thumb

You will not go far wrong by choosing between no baseline period, or a baseline period half the length of the recruitment period, whichever leads to the smaller variance

A baseline period is not needed in the following situations:

$$\tau = 1.0: m\rho \leq 1$$

$$\tau = 0.5: m\rho \leq 2$$

$$\tau = 0.1: m\rho \leq 5$$

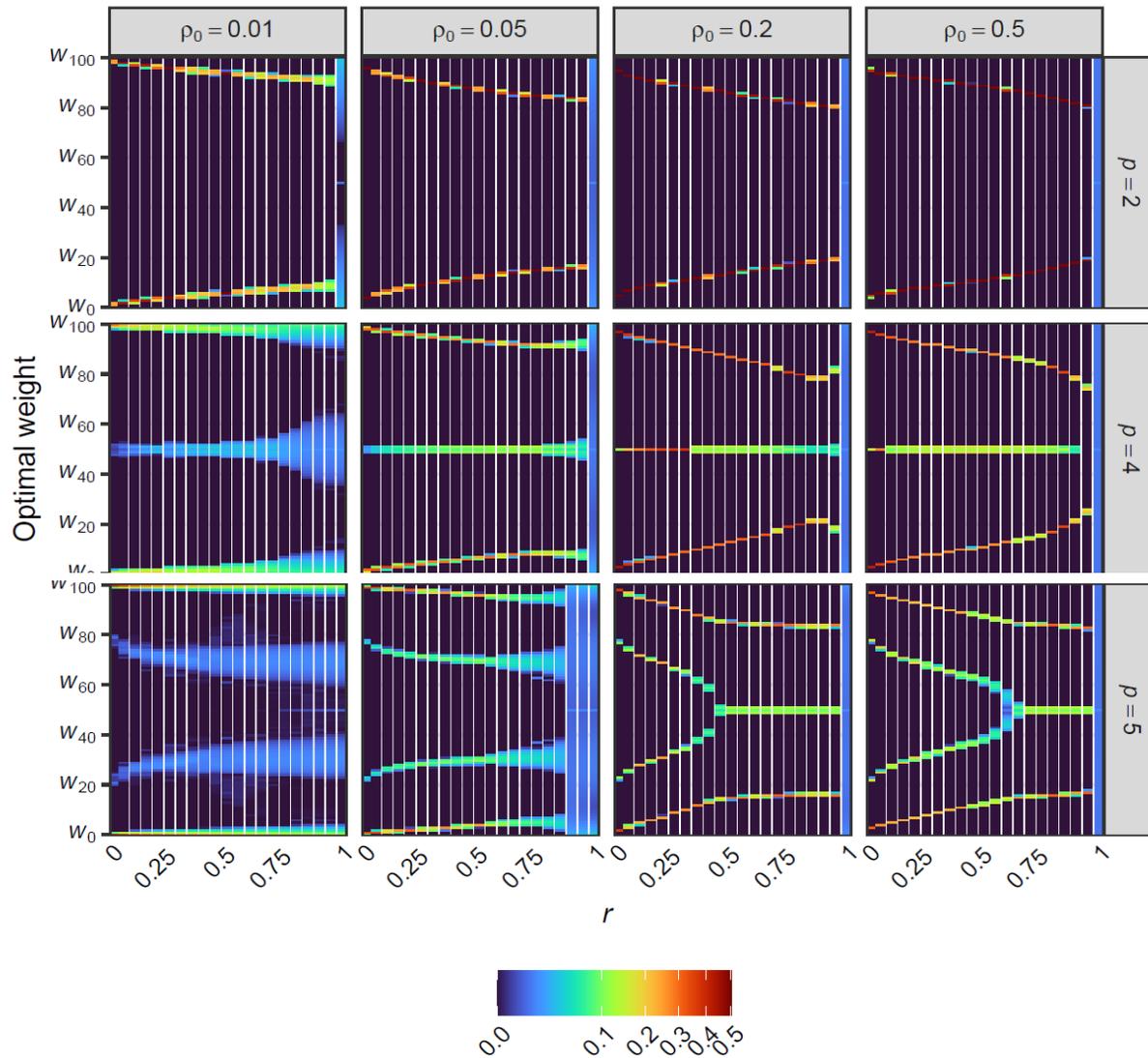
- Complete stepped wedge trials

# Optimal stepped-wedge cluster randomised trial designs for non-uniform correlation structures

Michael J. Grayling<sup>1</sup>, Richard Hooper<sup>2</sup>, Kim May Lee<sup>3</sup>

1. Population Health Sciences Institute, Newcastle University, Newcastle upon Tyne, UK
2. Pragmatic Clinical Trials Unit, Queen Mary University of London, London, UK
3. Institute of Psychiatry, Psychology & Neuroscience, King's College London, London, UK

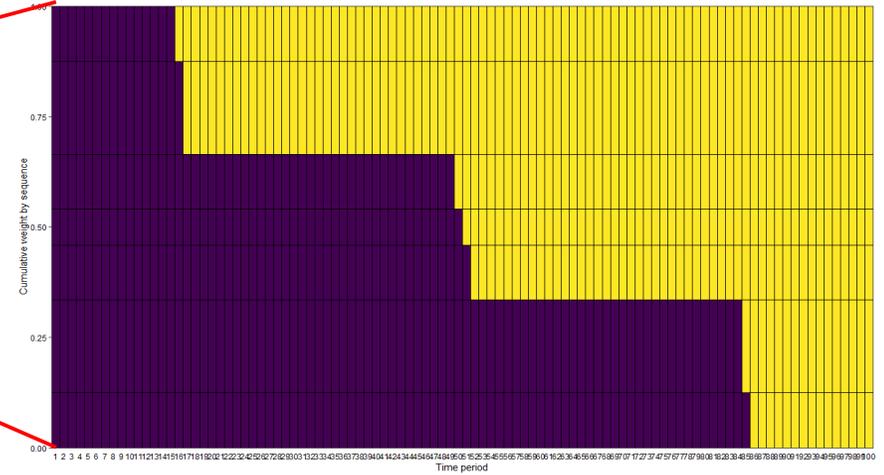
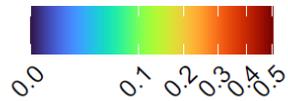
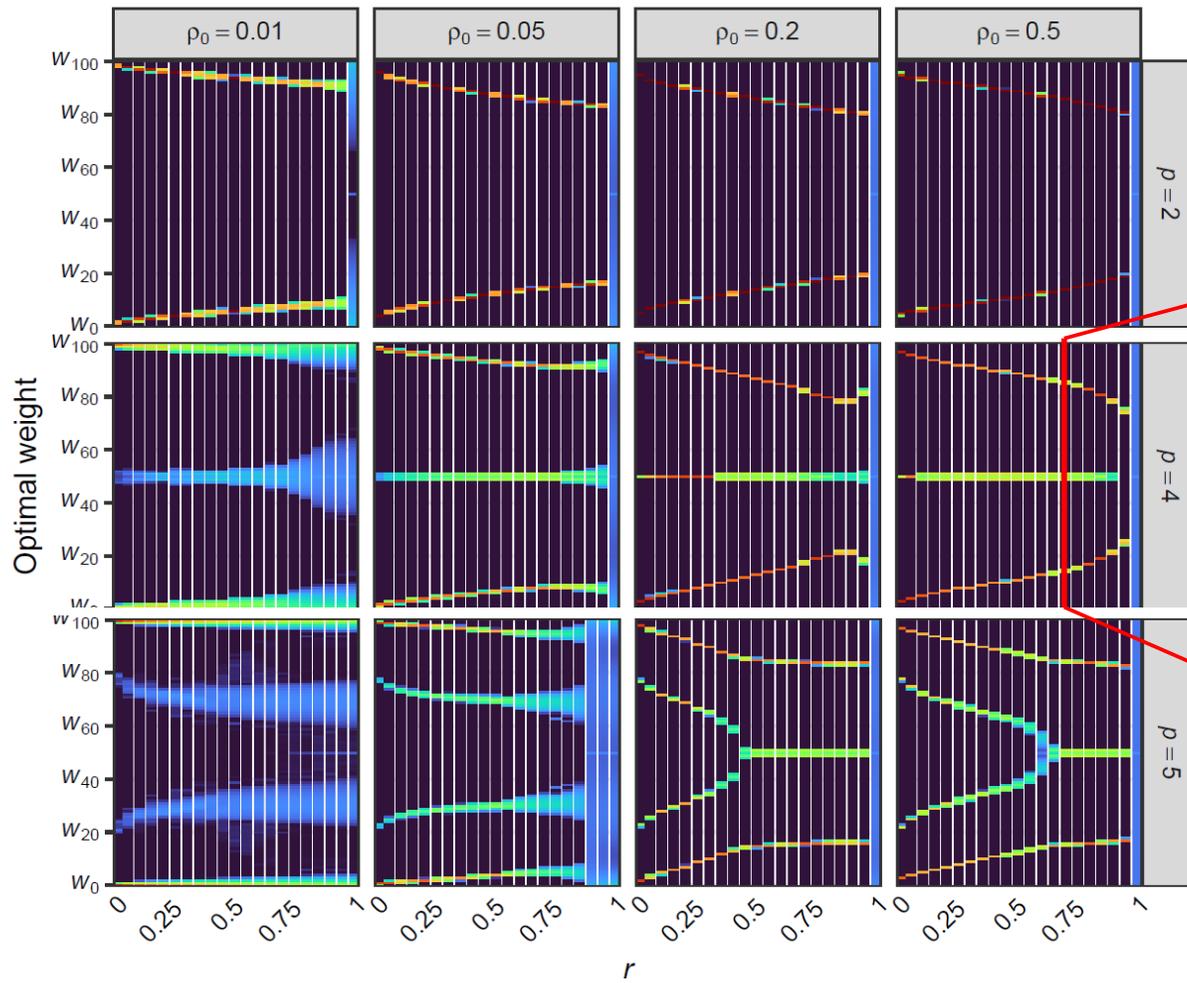
- Complete stepped wedge trials
  - $m = 100$
  - Regularised recruitment times  $1/100, 2/100, 3/100, \dots$
  - Number of clusters  $\gg 100$
  - How should we weight the clusters over the 101 possible cross-over sequences?

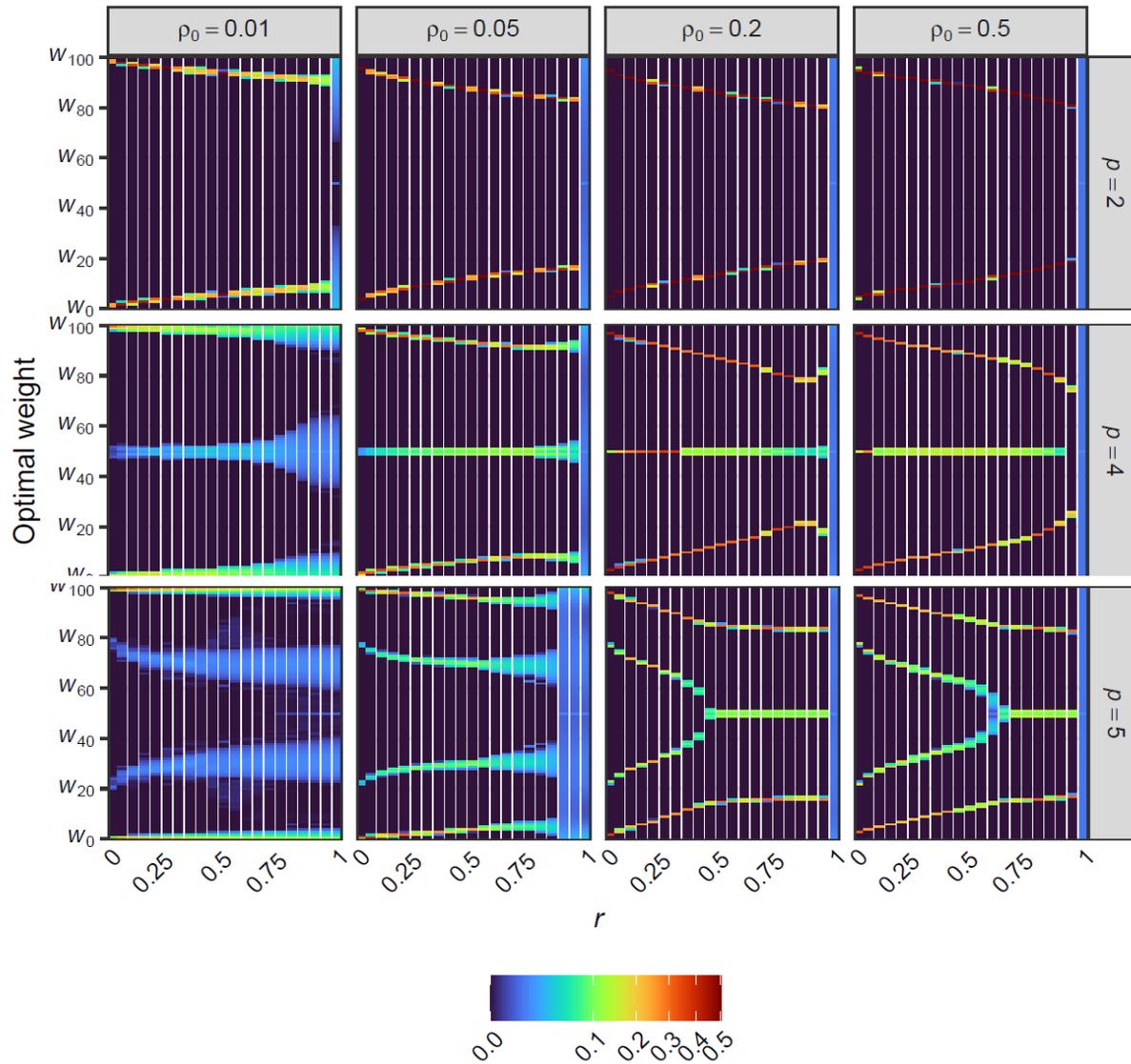


quadratic time effect

quartic time effect

quintic time effect





quadratic time effect

quartic time effect

quintic time effect

- Incomplete stepped wedge trials

RESEARCH ARTICLE

Open Access

# The hunt for efficient, incomplete designs for stepped wedge trials with continuous recruitment and continuous outcome measures

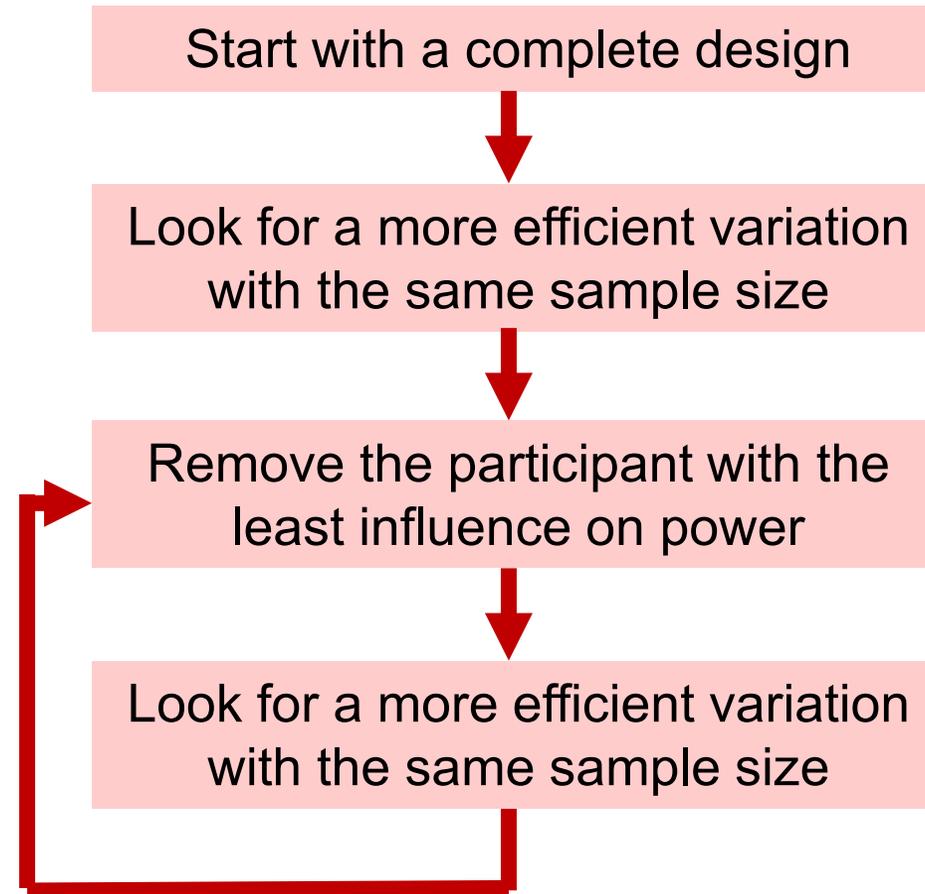


Richard Hooper<sup>1,2\*</sup> , Jessica Kasza<sup>3</sup> and Andrew Forbes<sup>3</sup>

- Incomplete stepped wedge trials



# Search algorithm

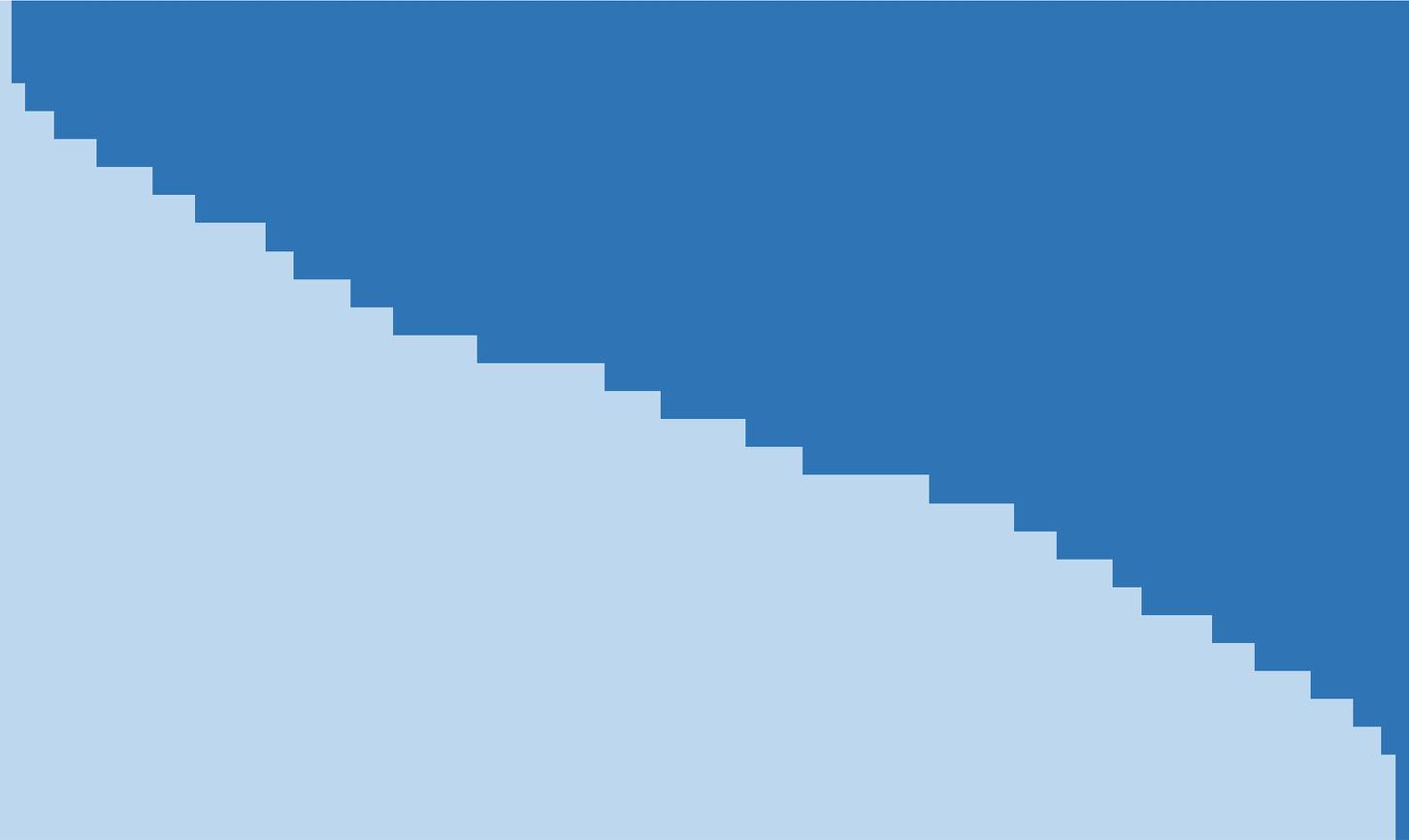


# Solutions

- 30 clusters,  $m = 100$
- Time effect modelled as a 6<sup>th</sup> order polynomial
- Designs achieving 90% power at the 5% significance level to detect the given effect size

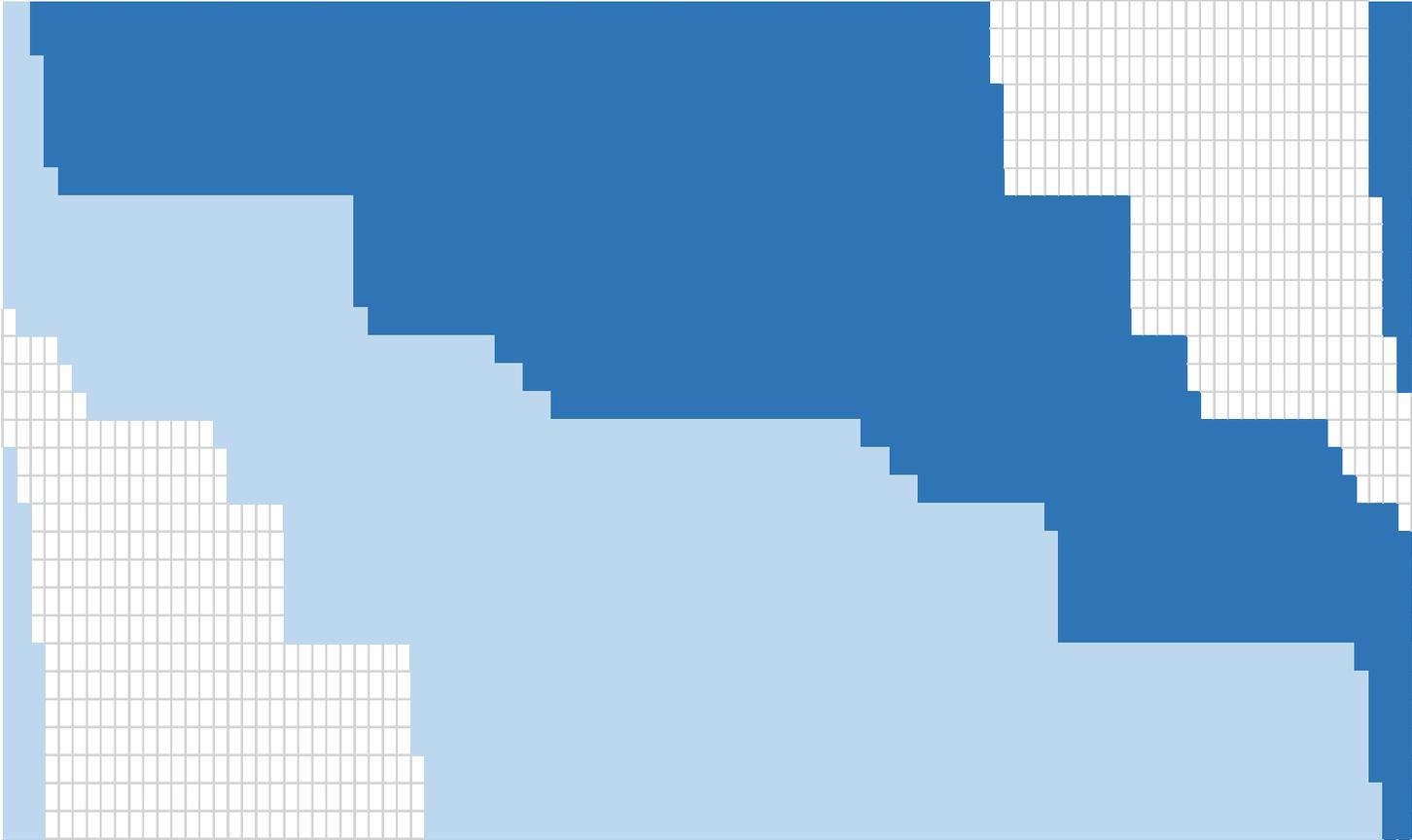
Effect size 0.15

$n = 3,000$



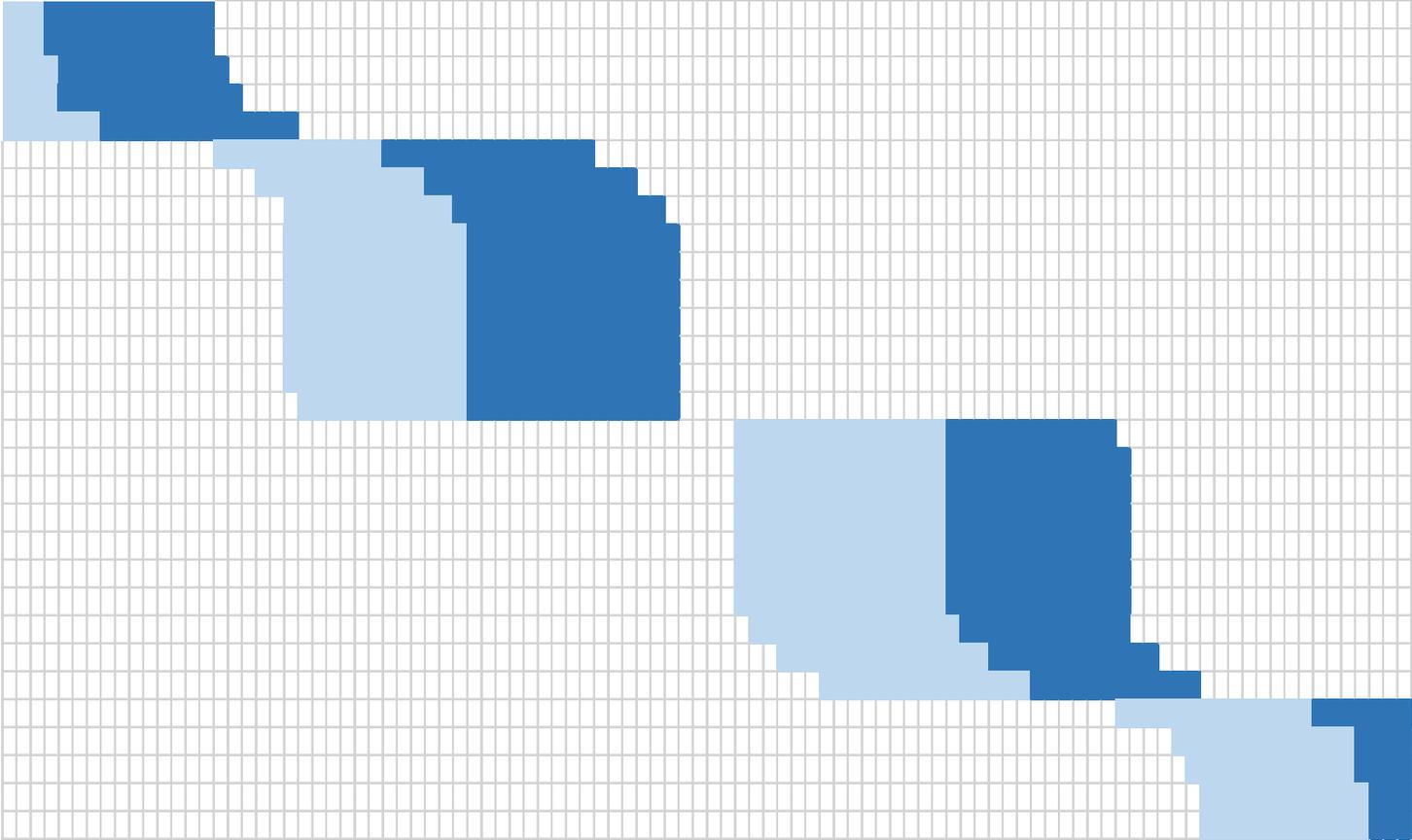
Effect size 0.20

$n = 2,328$



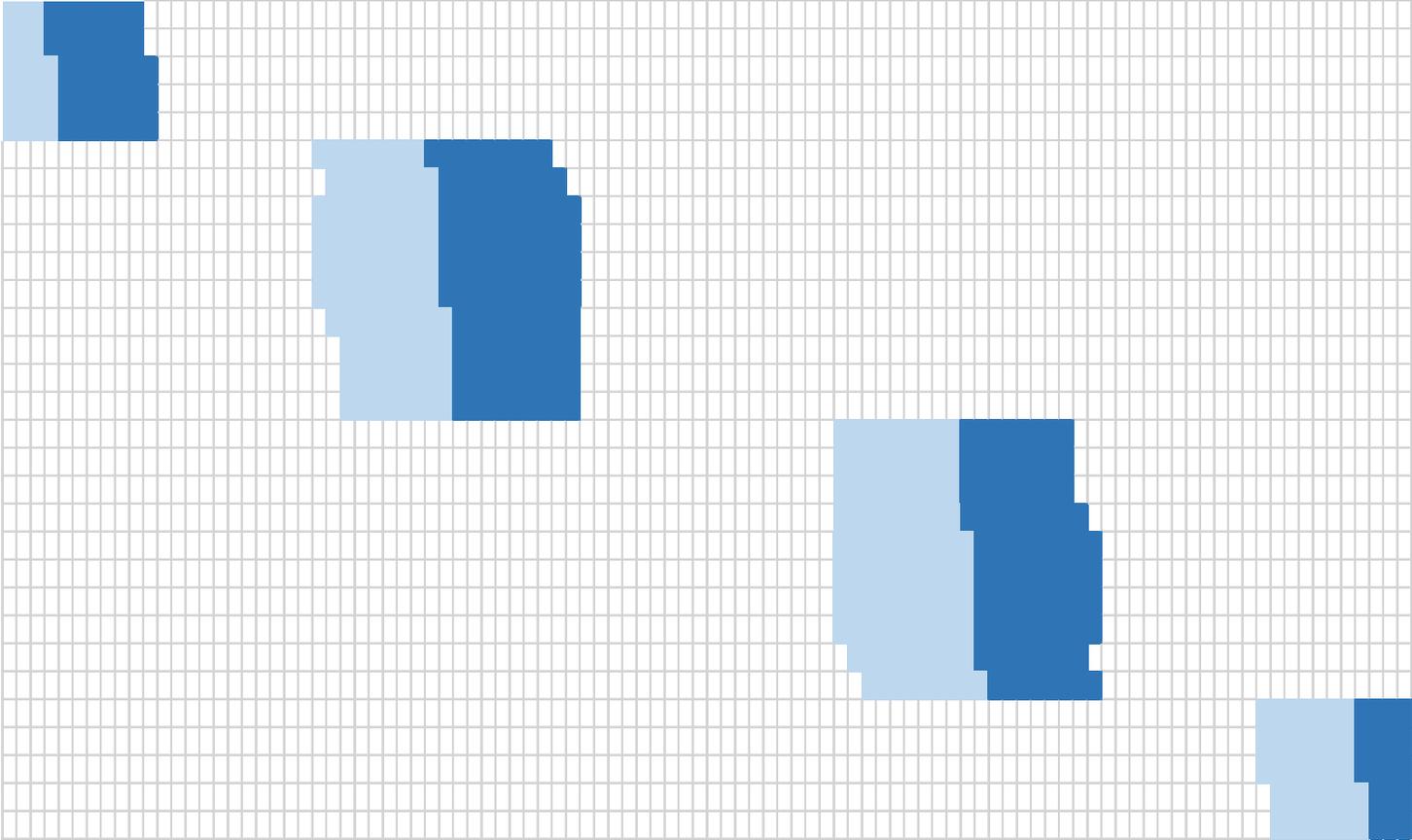
Effect size 0.25

$n = 720$



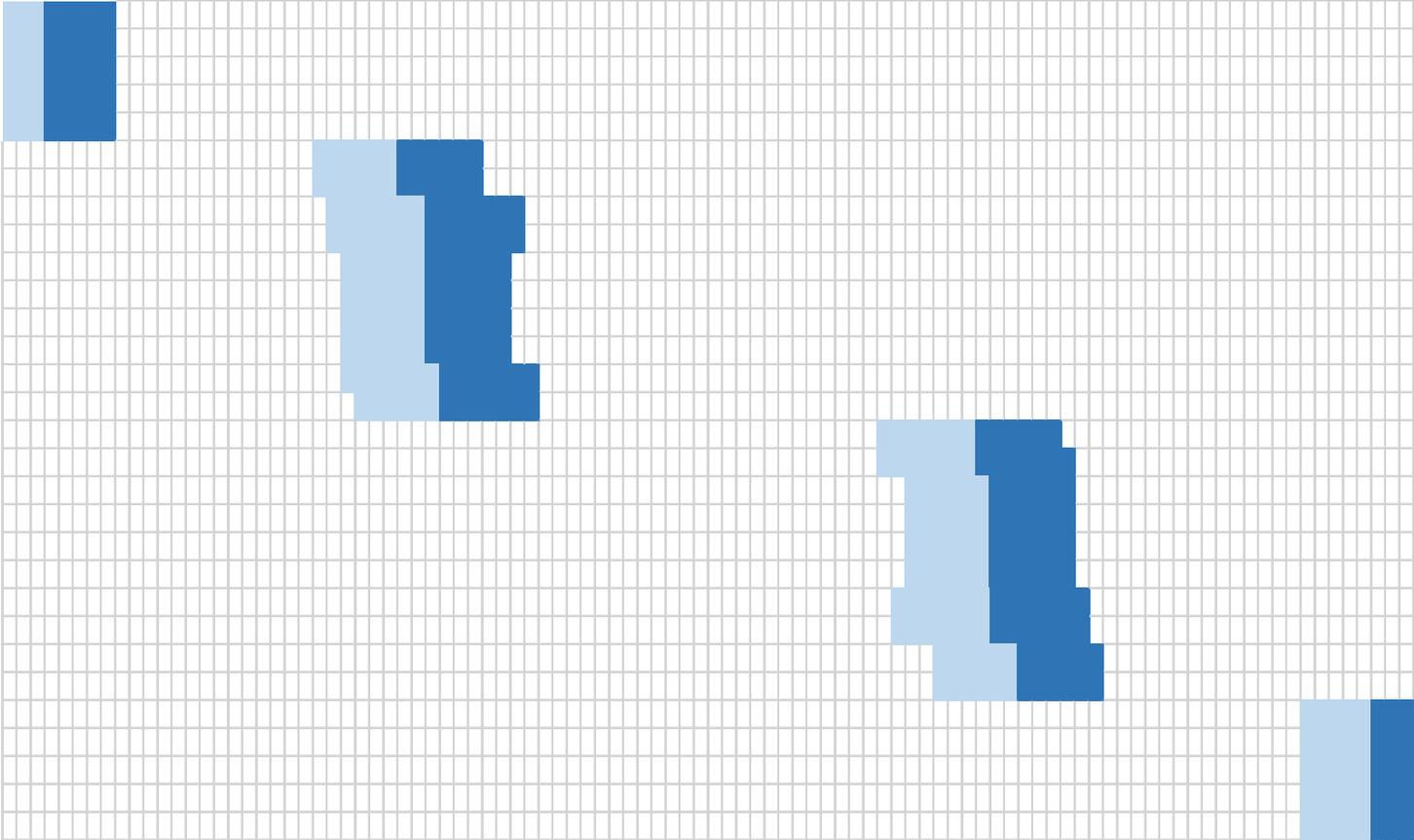
Effect size 0.30

$n = 464$



Effect size 0.35

$n = 334$



# Concluding remarks

## Concluding remarks

- Cluster randomised trials with a prospective baseline: you can follow a simple rule of thumb
- Complete stepped wedge trials: you could argue for keeping the number of steps small, even with a large number of clusters
- Incomplete stepped wedge trials: you could argue for randomising clusters to a series of non-overlapping interrupted time series
- The less “smooth” the time effect, the more steps you may need

# Concluding remarks

- I have ignored problems with small numbers of clusters: that's a whole other talk!
- Design needs new thinking, but analysis needs new software tools

8th ANNUAL MEETING



# CURRENT DEVELOPMENTS IN CLUSTER RANDOMISED TRIALS & STEPPED WEDGE DESIGNS

14-15  
NOVEMBER  
2022



Venue: Whitechapel Gallery, London, UK in-person, and also online

For more info: <https://www.qmul.ac.uk/pctu/courses-and-events/>

# References cited in this presentation

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# Other useful references

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# Questions?

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